

Summer
Scheme of learning

Year 6

**White
Rose
Maths**

#MathsEveryoneCan

The White Rose Maths schemes of learning

Teaching for mastery

Our research-based schemes of learning are designed to support a mastery approach to teaching and learning and are consistent with the aims and objectives of the National Curriculum.

Putting number first

Our schemes have number at their heart. A significant amount of time is spent reinforcing number in order to build competency and ensure children can confidently access the rest of the curriculum.

Depth before breadth

Our easy-to-follow schemes support teachers to stay within the required key stage so that children acquire depth of knowledge in each topic. Opportunities to revisit previously learned skills are built into later blocks.

Working together

Children can progress through the schemes as a whole group, encouraging students of all abilities to support each other in their learning.

Fluency, reasoning and problem solving

Our schemes develop all three key areas of the National Curriculum, giving children the knowledge and skills they need to become confident mathematicians.

Concrete – Pictorial – Abstract (CPA)

Research shows that all children, when introduced to a new concept, should have the opportunity to build competency by following the CPA approach. This features throughout our schemes of learning.

Concrete

Children should have the opportunity to work with physical objects/concrete resources, in order to bring the maths to life and to build understanding of what they are doing.



Pictorial

Alongside concrete resources, children should work with pictorial representations, making links to the concrete. Visualising a problem in this way can help children to reason and to solve problems.



Abstract

With the support of both the concrete and pictorial representations, children can develop their understanding of abstract methods.

An abstract representation of the addition problem 5 + 7. The equation is written inside a yellow rectangular box with a slight 3D effect.

If you have questions about this approach and would like to consider appropriate CPD, please visit www.whiterosemaths.com to find a course that's right for you.

Teacher guidance

Every block in our schemes of learning is broken down into manageable small steps, and we provide comprehensive teacher guidance for each one. Here are the features included in each step.

Notes and guidance that provide an overview of the content of the step and ideas for teaching, along with advice on progression and where a topic fits within the curriculum.

Things to look out for, which highlights common mistakes, misconceptions and areas that may require additional support.

Year 5 | Autumn Term | Block 1 – Place Value | Step 1

Roman numerals to 1,000

Notes and guidance

In Year 4, children learned about Roman numerals to 100. In this small step, they explore Roman numerals to 1,000, and the symbols D (500) and M (1,000) are introduced. Children explore further the similarities and differences between the Roman number system and our number system, learning that the Roman system does not have a zero and does not use placeholders. Children use their knowledge of M and D to recognise years using Roman numerals. Asking children to write the date in Roman numerals is one way to reinforce the concept daily.

Things to look out for

- Children may mix up which letter stands for which number.
- Children may add the individual values together instead of interpreting the values based on their position, for example interpreting CD as 600 instead of 400
- It is often more difficult to convert numbers that require large strings of Roman numerals.
- Children may think that numbers such as 990 can be written as XM instead of CMXC.

Key questions

- What patterns can you see in the Roman number system?
- What rules do we use when converting numbers to Roman numerals?
- What letters are used in the Roman number system? What does each letter represent?
- How do you know what order to write the letters when using Roman numerals?
- What is the same and what is different about representing the number “five hundred and three” in the Roman number system and in our number system?

Possible sentence stems

- The letter _____ represents the number _____
- I know _____ is greater than _____ because _____

National Curriculum links

- Read Roman numerals to 1,000 (M) and recognise years written in Roman numerals

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Key questions that can be posed to children to develop their mathematical vocabulary and reasoning skills, digging deeper into the content.

Possible sentence stems to further support children’s mathematical language and to develop their reasoning skills.

National Curriculum links to indicate the objective(s) being addressed by the step.




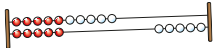
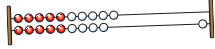




Teacher guidance

A **Key learning** section, which provides plenty of exemplar questions that can be used when teaching the topic.

Year 2 | Autumn Term | Block 1 - Place Value | Step 1

Numbers to 20

Key learning

- Complete the number tracks.
 - 0 1 2
 - 10 11 12
 - 7 8 13
- What numbers are shown?
 -   
 - Give your answers in numerals and words.
- What number is shown on each Rekenrek?
 - 
 - 
 - Give your answers in numerals and words.
- What numbers are shown?
 -    
 - Give your answers in numerals and words.
- Use words to complete the sentences.
 - The number after four is _____
 - The number before eight is _____
 - The number after nine is _____
- Make each number in three different ways.
 - 19 fifteen 16 eleven

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Activity symbols that indicate an idea can be explored practically

Reasoning and problem-solving activities and questions that can be used in class to provide further challenge and to encourage deeper understanding of each topic.

Year 3 | Autumn Term | Block 1 - Place Value | Step 4

Hundreds

Reasoning and problem solving

I am going to count in 100s from zero.

Dora

Write two numbers that Dora will say.

any two multiples of 100

No

Mo is counting in hundreds.

... 8 hundred, 9 hundred, 10 hundred

Mo should have said 1 thousand, 10 hundreds is equal to 1 thousand.

How should Mo have said the last number?

Dora will say the number 160

Tiny

Is Tiny correct? How do you know?

Balloons come in bags of 10

Rosie has 300 balloons.

Rosie has 30 bags of balloons.

How many bags does she have?

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Answers provided where appropriate

Activities and symbols

Key Stage 1 activities

Key Stage 1 includes more hands-on activities alongside questions.

An activity to be led by the teacher



Use a Rekenrek in the ready position.

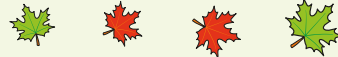


Ask children to show a number on their Rekenrek.

An outside activity or one that uses resources from nature



Find some seeds and leaves to represent Autumn.



Ask children to sort the objects in three different ways and then compare their answers with a partner.

An activity introduced by a reading from an appropriate fiction or non-fiction book



Read *The Button Box* by M Reid.

Give children a selection of buttons and ask them to sort the buttons in as many different ways as they can.

Encourage them to think about size, shape, colour and number of holes.

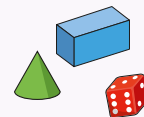


An investigation



Give children a selection of 3D shapes.

Ask children to sort the objects into two groups and then challenge a partner to say how the objects have been sorted.



Key Stage 1 and 2 symbols

The following symbols are used to indicate:



concrete resources might be useful to help answer the question



a bar model might be useful to help answer the question



drawing a picture might help children to answer the question



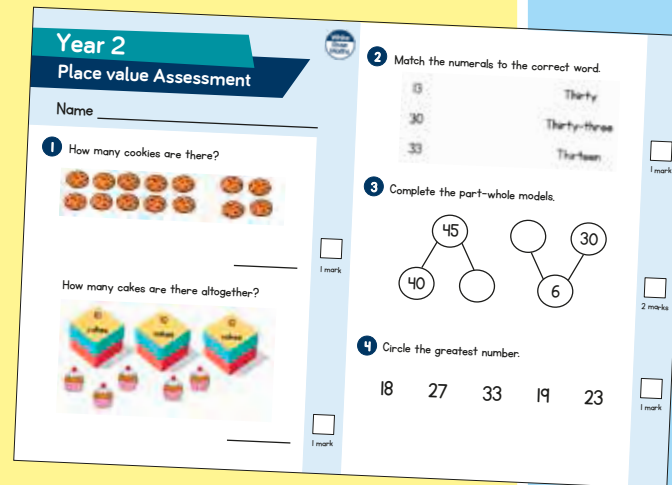
children talk about and compare their answers and reasoning



a question that should really make children think. The question may be structured differently or require a different approach from others and/or tease out common misconceptions.


Free supporting materials


End-of-block assessments to check progress and identify gaps in knowledge and understanding.



Year 2
Place value Assessment

Name _____

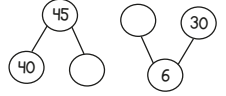
1 How many cookies are there?

_____ 1 mark

How many cakes are there altogether?

_____ 1 mark

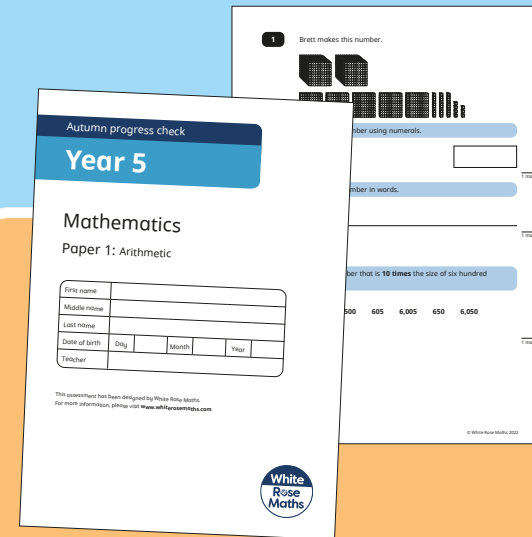
2 Match the numerals to the correct word.

13	Thirty
30	Thirty-three
33	Thirteen

_____ 1 mark

3 Complete the part-whole models.

_____ 2 marks

4 Circle the greatest number.
18 27 33 19 23
_____ 1 mark



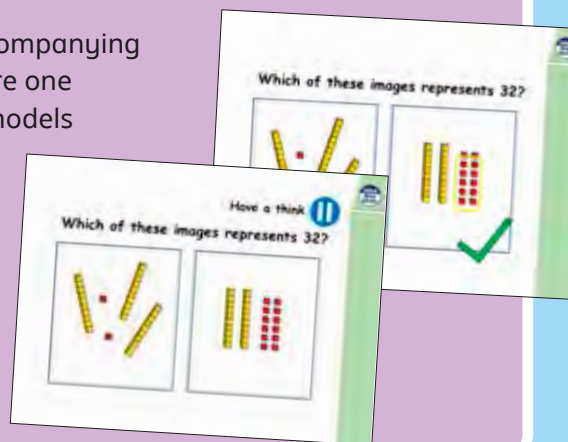
Autumn progress check
Year 5
Mathematics
Paper 1: Arithmetic


First name			
Middle name			
Last name			
Date of birth	Day	Month	Year
Teacher			


This assessment has been designed by White Rose Maths. For more information, please visit www.white-rose-maths.com

White Rose Maths

Each small step has an accompanying **home learning video** where one of our team of specialists models the learning in the step. These can also be used to support students who are absent or who need to catch up content from earlier blocks or years.



Which of these images represents 32?


Have a think
Which of these images represents 32?


End-of-term assessments for a more summative view of where children are succeeding and where they may need more support.

Free supporting materials

Primary Progression – Place Value						
	Year 1	Year 2	Year 3	Year 4	Year 5	Year 6
Place Value: Counting	<ul style="list-style-type: none"> count to and across 100, forwards and backwards, beginning with 0 or 1, or from any given number Count numbers to 100 in numerals; count in multiples of twos, fives and tens <p>Autumn 1 Autumn 4 Spring 2 Summer 4</p>	<ul style="list-style-type: none"> count in steps of 2, 3, and 5 from 0, and in tens from any number, forward and backward <p>Autumn 1</p>	<ul style="list-style-type: none"> count from 0 in multiples of 4, 8, 50 and 100, find 10 or 100 more or less than a given number <p>Autumn 1 Autumn 3</p>	<ul style="list-style-type: none"> count in multiples of 6, 7, 9, 25 and 1000 count backwards through zero to include negative numbers <p>Autumn 1 Autumn 4</p>	<ul style="list-style-type: none"> count forwards or backwards in steps of powers of 10 for any given number up to 1 000 000 count forwards and backwards with positive and negative whole numbers, including through zero <p>Autumn 1</p>	

National Curriculum progression to indicate how the schemes of learning fit into the wider picture and how learning progresses within and between year groups.

Skill: Add three 1-digit numbers

Year: 2

When adding three 1-digit numbers, children should be encouraged to look for number bonds to 10 or doubles to add the numbers more efficiently.

This supports children in their understanding of commutativity.

Manipulatives that highlight number bonds to 10 are effective when adding three 1-digit numbers.

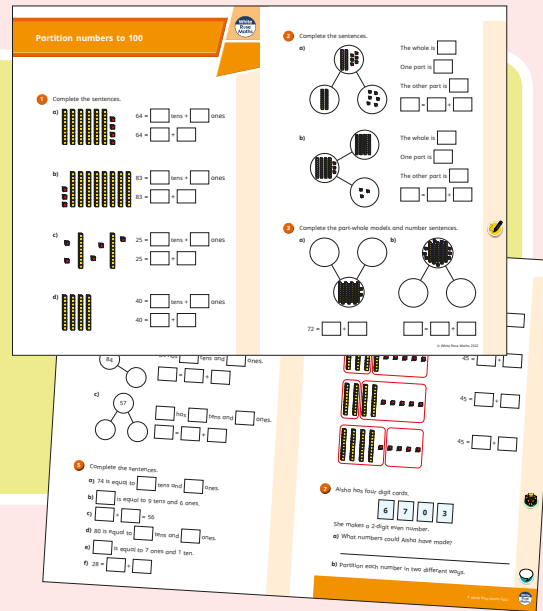
Calculation policies that show how key approaches develop from Year 1 to Year 6.

Ready to Progress – Number Facts Year 3			
	3NF-1	3NF-2	3NF-3
RTP Criteria	Secure fluency in addition and subtraction facts that bridge 10, through continued practice.	Recall multiplication facts, and corresponding division facts, in the 10, 5, 2, 4 and 8 multiplication tables, and recognise products in these multiplication tables as multiples of the corresponding number.	Apply place-value knowledge to know additive and multiplicative number facts (scaling facts by 10).
White Rose Maths Small Steps	Autumn 2 Addition and Subtraction <ul style="list-style-type: none"> Add 3-digit and 1-digit numbers - crossing 10 Subtract a 1-digit number from a 3-digit number - crossing 10 Add 3-digit and 2-digit numbers - crossing 100 Subtract a 2-digit number from a 3-digit number - crossing 100 	Autumn 3 Multiplication and Division <ul style="list-style-type: none"> 2 times-table 5 times-table Divide by 2 Divide by 5 Divide by 10 Multiply by 4 Divide by 4 The 4 times-table Multiply by 8 Divide by 8 The 8 times-table 	Spring 1 Multiplication and Division <ul style="list-style-type: none"> Related calculations Scaling Spring 4 Measurement: Length and Perimeter <ul style="list-style-type: none"> Equivalent lengths (m and cm) Equivalent lengths (mm and cm)

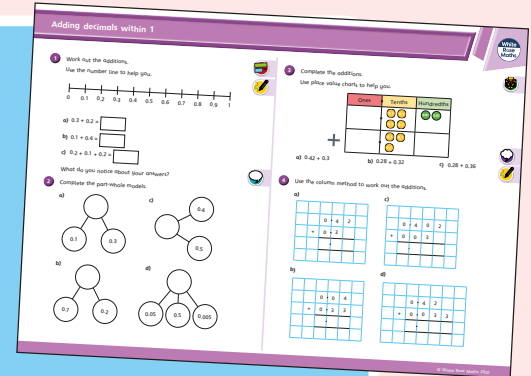
Ready to progress mapping that shows how the schemes of learning link to curriculum prioritisation.

Premium supporting materials

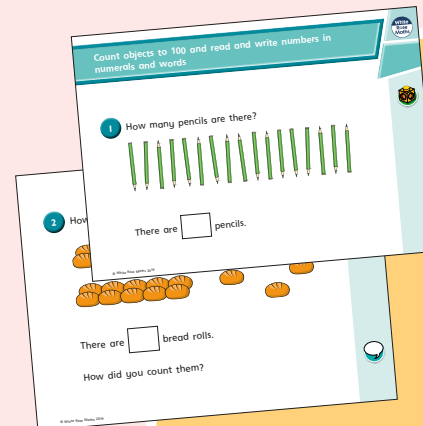
Worksheets to accompany every small step, providing relevant practice questions for each topic that will reinforce learning at every stage.



Display versions of the worksheet questions for front of class/whole class teaching.

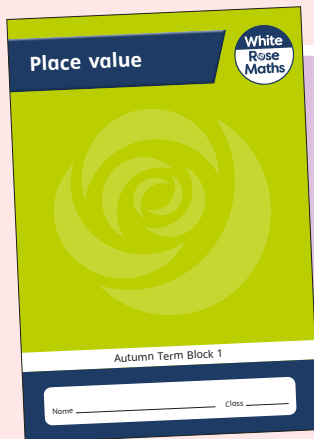


PowerPoint™ versions of the worksheet questions to incorporate them into lesson planning.



Answers to all the worksheet questions.

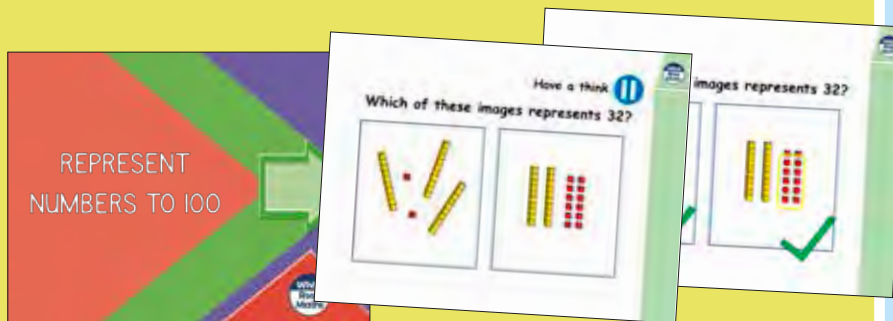
Question	Answer
1	There are 17 pencils.
2	There are 14 bread rolls. Children may have counted 3 tens and 1 roll.
3	twenty-eight
4	sixty-two
5	4 tens and 5 ones
6	a) seventeen b) twenty-one c) thirty-five d) eighty-two
7	a) 12 b) 80 c) 100 d) 9 e) 27 f) 14
8	79, 80, 81, 82, 83, 85 70, 79, 66, 64, 63
9	Eric has 20 sweets. Ed's friend gives her 7 sweets.



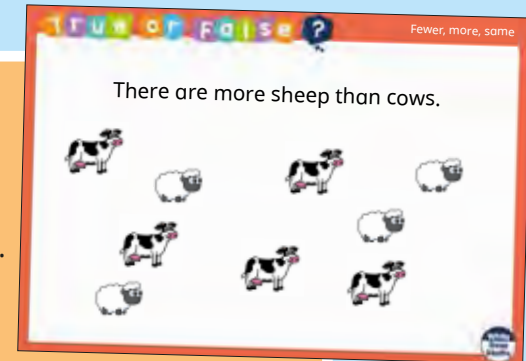
Also available as printed **workbooks**, per block.

Premium supporting materials

Teaching slides that mirror the content of our home learning videos for each step. These are fully animated and editable, so can be adapted to the needs of any class.

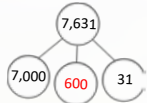


A **true or false** question for every small step in the scheme of learning. These can be used to support new learning or as another tool for revisiting knowledge at a later date.



Flashback 4 starter activities to improve retention. Q1 is from the last lesson; Q2 is from last week; Q3 is from 2 to 3 weeks ago; Q4 is from last term/year. There is also a bonus question on each one to recap topics such as telling the time, times-tables and Roman numerals.

Flashback 4 Year 4 | Week 5 | Day 1

- 1) Round 6,495 to the nearest 10, 100 and 1,000 5×2
6,500 6,500 6,000
- 2) Round 38 to the nearest 10 40
- 3) Complete the part-whole model.

- 4) Multiply 38 by 4 152



Topic-based CPD videos

As part of our on-demand CPD package, our maths specialists provide helpful hints and guidance on teaching topics for every block in our schemes of learning.

Meet the characters

Our class of characters bring the schemes to life, and will be sure to engage learners of all ages and abilities. Follow the children and their class pet, Tiny the tortoise, as they explore new mathematical concepts and ideas.

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Maths



Yearly overview

The yearly overview provides suggested timings for each block of learning, which can be adapted to suit different term dates or other requirements.

	Week 1	Week 2	Week 3	Week 4	Week 5	Week 6	Week 7	Week 8	Week 9	Week 10	Week 11	Week 12
Autumn	Number Place value		Number Addition, subtraction, multiplication and division				Number Fractions A		Number Fractions B		Measurement Converting units	
Spring	Ratio		Algebra		Number Decimals		Number Fractions, decimals and percentages		Measurement Area, perimeter and volume		Statistics	
Summer	Geometry Shape			Geometry Position and direction	Themed projects, consolidation and problem solving							

Summer Block 1

Shape

Small steps

Step 1

Measure and classify angles

Step 2

Calculate angles

Step 3

Vertically opposite angles

Step 4

Angles in a triangle

Step 5

Angles in a triangle – special cases

Step 6

Angles in a triangle – missing angles

Step 7

Angles in a quadrilateral

Step 8

Angles in polygons

Small steps

Step 9

Circles

Step 10

Draw shapes accurately

Step 11

Nets of 3-D shapes

Measure and classify angles

Notes and guidance

In Year 4, children encountered the classifications of angles as acute, right and obtuse. In Year 5, this learning was extended to include the use of degrees, as well as reflex angles. This small step revisits that learning by classifying angles and measuring them with a protractor.

Begin by recapping the types of angles. Move on to using a protractor to measure an angle, taking care when modelling which scale to use. Encourage children to estimate the size of an angle before measuring it, as they are then less likely to read the wrong scale on the protractor. For example, if an angle is seen to be less than a right angle, its size will be less than 90° . Children should practise estimating angles by comparing them to known fractions of a turn.

Similarly, classifying angles first can support children in reading the correct scale. For example, if an angle is acute, then the size of the angle in degrees must be less than 90

Things to look out for

- Children may read the scale on the protractor from the wrong end.
- Children may require support when measuring reflex angles with a 180° protractor.

Key questions

- What are the four types of angles?
- How many degrees are there in a right angle?
- How can you describe an acute/obtuse/reflex angle?
- How can you use a protractor to measure an angle? Where on the angle do you place the protractor?
- Does it matter which end of the protractor you start from?
- How can you use a protractor to measure a reflex angle?

Possible sentence stems

- The angle is _____ than _____ of a turn.
It is a/an _____ angle.
- A/an _____ angle is between _____ and _____ degrees.

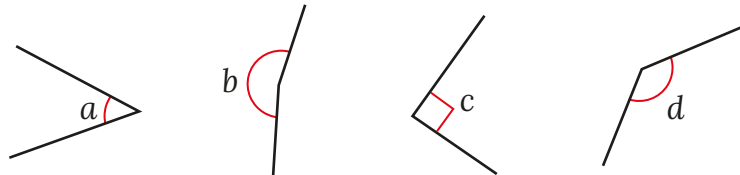
National Curriculum links

- Recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles
- Draw given angles, and measure them in degrees ($^\circ$) (Y5)
- Know angles are measured in degrees: estimate and compare acute, obtuse and reflex angles (Y5)

Measure and classify angles

Key learning

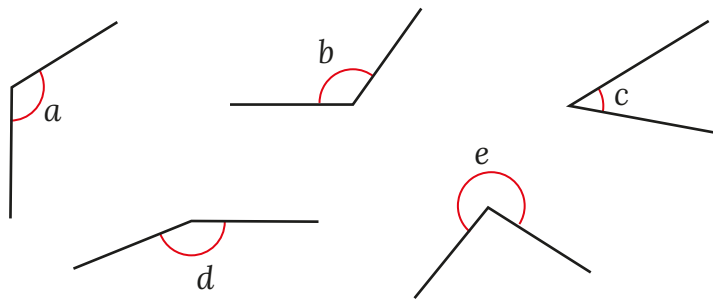
- For each angle, choose a word to complete the sentence.



Angle _____ is a/an _____ angle.

Order the angles from smallest to greatest.

- Use a protractor to measure each angle, then complete the sentences.



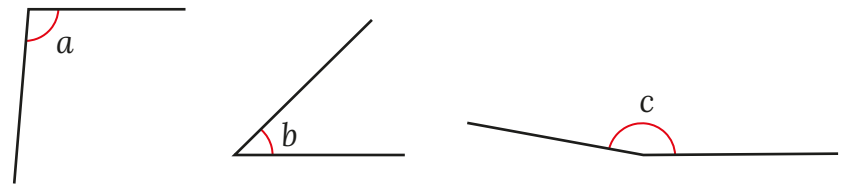
Angle _____ is _____ degrees.

It is a/an _____ angle.

- Nijah knows that this angle is slightly smaller than a right angle, so she estimates that it is approximately 85°.



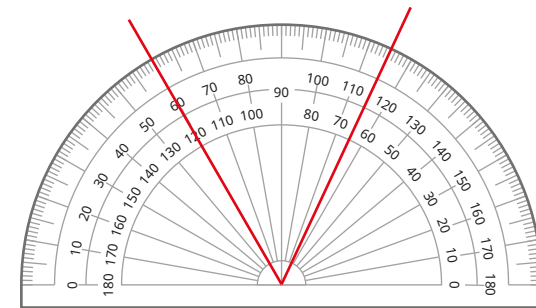
Estimate the sizes of these angles.



Now measure them with a protractor.

How close were your estimates?

- What is the size of this angle?



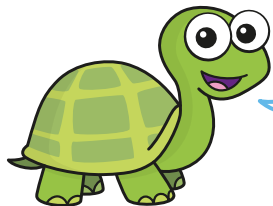
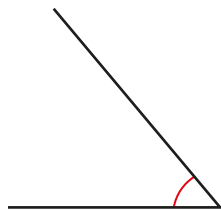
How did you work out your answer?

How else could you measure the angle?

Measure and classify angles

Reasoning and problem solving

Tiny is measuring angles.



This angle is 130° .

The angle is acute.

Tiny could have used the wrong scale.

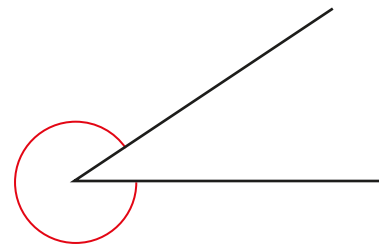
50°

Explain why Tiny must be wrong.

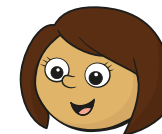
What mistake could Tiny have made?

What could the angle measure?

Kim is trying to measure the size of this reflex angle.



The protractor only measures 180° and this is greater than that, so I cannot measure it.



No

Do you agree with Kim?

Explain your answer.



Calculate angles

Notes and guidance

In Year 5, children learnt that angles on a straight line add up to 180° and angles around a point add up to 360° . That learning is revisited in this small step, with children calculating missing angles from given information.

Children also need to know the symbol for a right angle, and that an angle marked with this symbol measures 90° . They should recognise that without this symbol the size of the angle cannot be assumed.

Children start by calculating missing angles within a right angle, using mental or written strategies to subtract the given angle(s) from 90° . They then revisit angles on a straight line and angles around a point. Children should explore both methods: subtracting each known part from the whole in turn; and adding the known parts together and subtracting this from the whole.

Things to look out for

- Children may try to find missing angles by measuring with a protractor, rather than working them out using given facts.
- Children may make errors when using mental strategies of subtraction, for example $90 - 75 = 25$

Key questions

- How can you calculate angles without using a protractor?
- What sort of angle is shown by a square marker?
- What do angles within a right angle add up to?
- What do angles on a straight line add up to?
- What do angles around a point add up to?
- Which angles are already given?
How can you use these to calculate the missing angle?
- Is there more than one way to work out the answer?

Possible sentence stems

- Angles in a right angle add up to _____ $^\circ$.
- Angles on a straight line add up to _____ $^\circ$.
- Angles around a point add up to _____ $^\circ$.
- The total of angle _____ and angle _____ is _____ $^\circ$.
To find angle _____, subtract _____ from _____

National Curriculum links

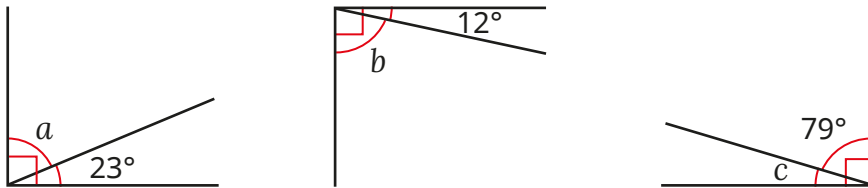
- Recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles

Calculate angles

Key learning

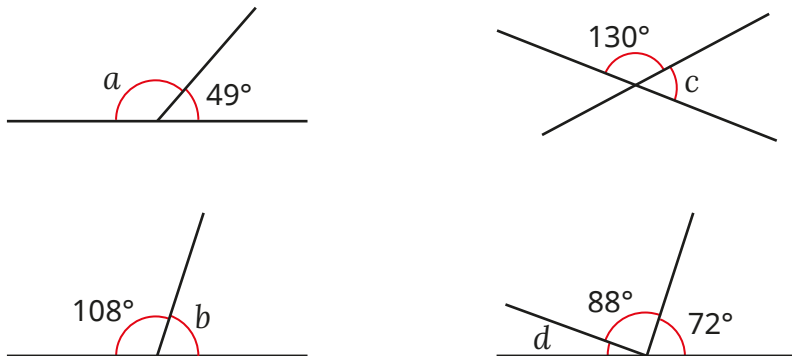
- A right angle measures 90° .

Use this fact to work out the sizes of angles a , b and c .



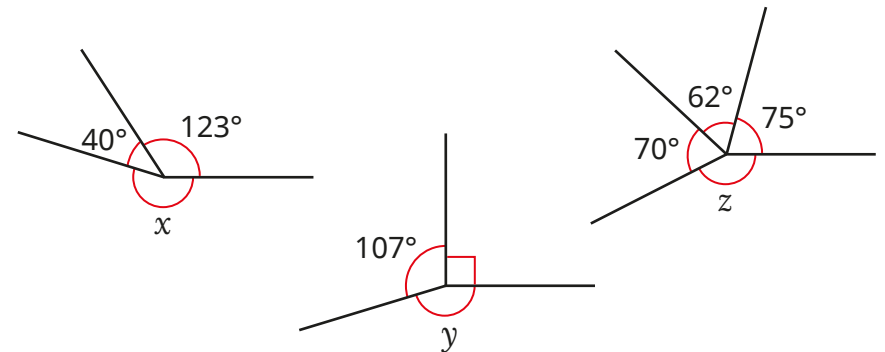
- Angles on a straight line add up to 180° .

Use this fact to work out the sizes of the angles marked with letters.

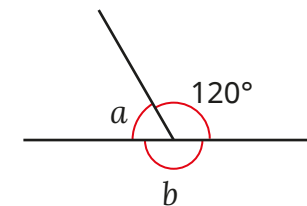


- Angles around a point add up to 360° .

Use this fact to work out the sizes of the angles marked with letters.



- Here are three angles on a straight line.



Which of these statements are true?

$a < b$

$a + 120^\circ = b$

$b - a = 120^\circ$

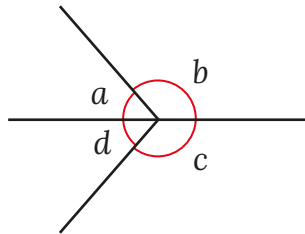
a is half the size of 120° .

$a + b = 120^\circ$

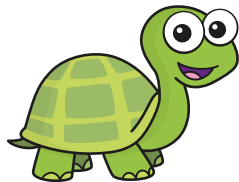
Calculate angles

Reasoning and problem solving

Tiny is investigating angles around a point.



I know that $a + b + c + d = 360^\circ$, so angles a , b and c could each be 100° and d could be 60° .

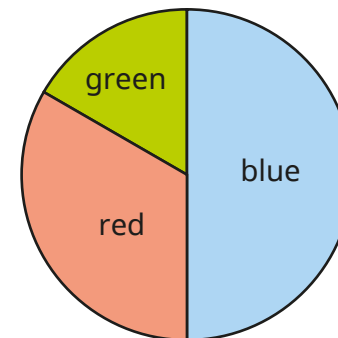


Do you agree with Tiny?
Explain your answer.



No

Here is a pie chart showing the colours of cars sold by a car dealer.



blue: 180°
red: 120°
green: 60°

The number of blue cars sold is equal to the total number of red and green cars sold.

The dealer sold twice as many red cars as green cars.

Work out the size of the angle for each sector of the pie chart.

Vertically opposite angles

Notes and guidance

In this small step, children learn that vertically opposite angles are equal. Begin by showing what vertically opposite angles are. By drawing two straight lines that intersect at a point, four angles are created. Through investigation, children see that there are two pairs of equal angles. They need to understand that vertically opposite angles are formed when two straight lines cross, and if either of the lines are not straight, then the angles formed are not vertically opposite. Secure this understanding by comparing vertically opposite angles to pairs of angles around a point that are opposite each other, but not vertically opposite, i.e. they are not formed by two straight lines intersecting.

Once children understand that vertically opposite angles are equal, they can use this fact alongside the rules they already know to work out missing angles.

Things to look out for

- Children may think that vertically opposite angles must be vertical in relation to each other, rather than sharing a common vertex.
- Children may think that all opposite angles are equal, rather than only those formed by intersecting straight lines.

Key questions

- What are vertically opposite angles?
- How do you know that the angles are vertically opposite?
- Which angles are the same size? How do you know?
- What number sentences can you write about vertically opposite angles?
- How can you find the size of the missing angle?
Is there more than one way?
- What is the difference between vertically opposite angles and two angles around a point that are opposite each other?

Possible sentence stems

- Vertically opposite angles are _____
- If angle _____ is _____°, then angle _____ is also _____°.
- Angles _____ and _____ are equal, because ...

National Curriculum links

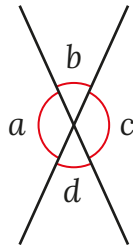
- Recognise angles where they meet at a point, are on a straight line, or are vertically opposite, and find missing angles

Vertically opposite angles

Key learning

- Take a piece of paper and draw a large “X”.

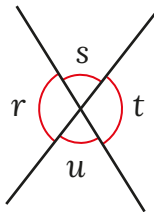
- ▶ Mark the angles on as shown.
- ▶ Measure each angle.
- ▶ What do you notice about angles b and d ?



What do you notice about angles a and c ?

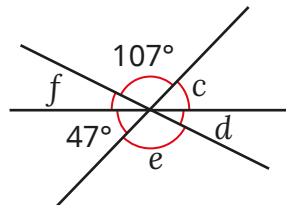
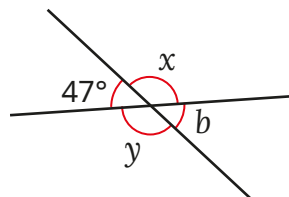
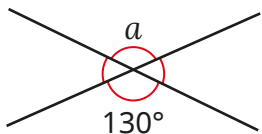
Is this always the case? Draw other “X” shapes to investigate.

- Use the letters from the diagram to complete the statements.

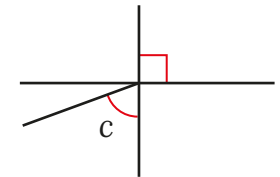
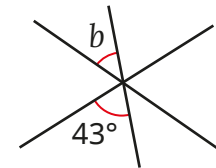
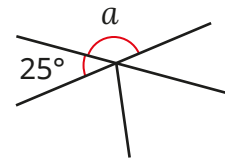


$$\begin{aligned} \underline{\hspace{2cm}} &= \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} + \underline{\hspace{2cm}} &= 180^\circ \\ \underline{\hspace{2cm}} &= \underline{\hspace{2cm}} \\ \underline{\hspace{2cm}} + \underline{\hspace{2cm}} &= 180^\circ \end{aligned}$$

- Work out the sizes of the angles marked with letters.



- Each diagram has been drawn using three straight lines.

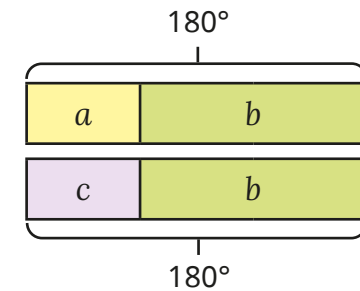
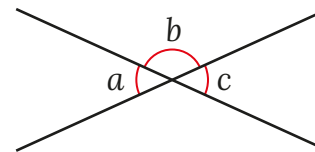


Which of the angle(s) marked with letters can you work out?

Which angle(s) can you not work out?

Talk about it with a partner.

- Brett has drawn a bar model to show the sizes of the angles.

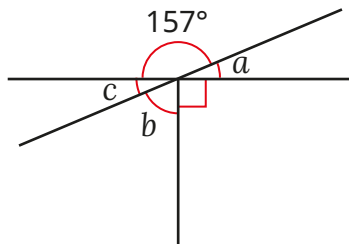


Explain how Brett’s bar model shows that angles a and c are the same size.

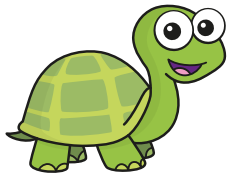
Vertically opposite angles

Reasoning and problem solving

This diagram is drawn using three straight lines.

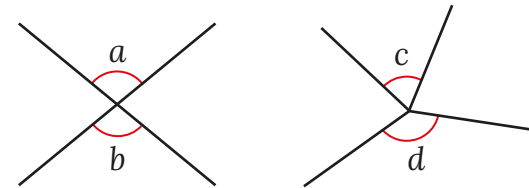


I only have enough information to work out the size of angle a .



Do you agree with Tiny?
Explain your answer.

No
 $a = 23^\circ$
 $b = 67^\circ$
 $c = 23^\circ$



Are the statements true or false?

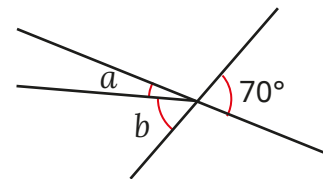
Angles a and b are equal.

Angles c and d are equal.

Explain your answer.

True
False

Three straight lines are drawn.



b is two and a half times greater than a .
Work out the size of angle a .

$a = 20^\circ$

Angles in a triangle

Notes and guidance

In this small step, children learn that the interior angles of a triangle always sum to 180° .

Get children to measure each angle of a triangle and add them together, doing this for a number of different triangles, in order to discover the rule. Discuss that, when using a protractor, there is the possibility of small inaccuracies causing the total to be slightly different from 180° .

When the rule is established, children work out unknown angles in triangles. They should see each angle as a “part” and 180° as the “whole”. The three parts add to make the whole. This means that they can work out one of the missing parts by subtracting each of the known parts from the whole, or adding the known parts together before subtracting this from the whole. This step is a good opportunity to revisit mental and written calculation methods, as well as using inverse operations to check answers.

Things to look out for

- Children may try to use a protractor to measure missing angles, rather than working them out based on given facts.
- Children may use 360° (from angles around a point) instead of 180° .

Key questions

- What does “interior” mean?
- How many interior angles does a triangle have?
- How can you measure the angles in a triangle?
- What do the interior angles of a triangle sum to?
- If you know the size of two interior angles in a triangle, how can you work out the third angle?
- Could you work out the missing angle a different way?

Possible sentence stems

- The angles in a _____ add up to _____ $^\circ$.
- The whole (180°) subtract the parts _____ $^\circ$ and _____ $^\circ$ gives the missing angle, _____ $^\circ$.

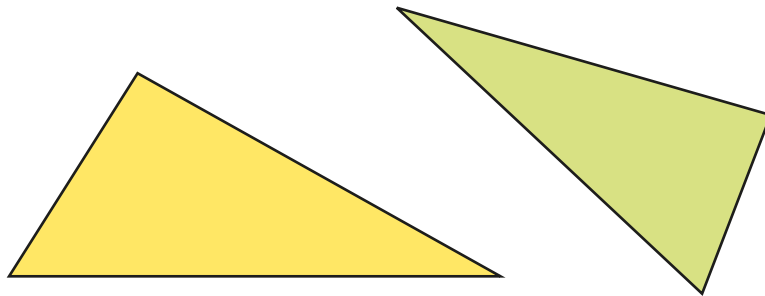
National Curriculum links

- Compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons

Angles in a triangle

Key learning

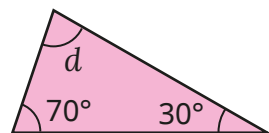
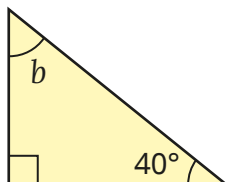
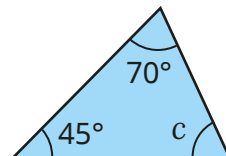
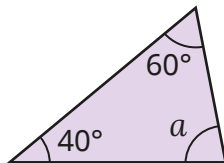
- Use a protractor to measure the angles in each triangle.



What is the sum of the angles in each triangle?

What do you notice?

- Calculate the sizes of the angles marked with letters.

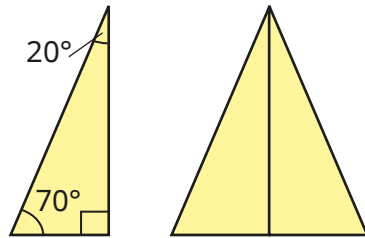


- Two angles in a triangle are 75° and 28° .
What is the size of the third angle?
- One angle in a right-angled triangle is 12° .
Find the sizes of the other two angles.
- Two angles in a triangle are 36.7° and 15.9° .
What is the size of the third angle?
- The first angle in a triangle is 42° .
The second angle is twice the size of the first angle.
What is the size of the third angle?
- A triangle has angles a , b and c .
Angle a is twice the size of angle b .
Angle b is three times the size of angle c .
What is the size of angle c ?

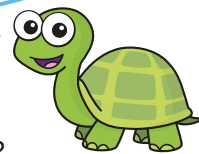
Angles in a triangle

Reasoning and problem solving

An isosceles triangle is made by combining two right-angled triangles.



The sum of the angles in the right-angled triangle is 180° , so the sum of the angles in the isosceles triangle must be 360° .



Do you agree with Tiny?
Explain your answer.

No

Are the statements true or false?

A triangle can have three acute angles.

A triangle can have two right angles.

A triangle must have at least one obtuse angle.

All three angles can be the same in a triangle.

If one of the angles in a triangle is a right angle, the other two angles must be the same as each other.

Explain your answers.

True
False
False
True
False

Angles in a triangle – special cases

Notes and guidance

In Year 4, children learnt to classify triangles as equilateral, isosceles or scalene, based on the lengths of their sides. They also know that a right-angled triangle has one angle of 90° . In this small step, children extend this learning to include the angles of triangles. Using their knowledge of angles in specific triangles, as well as the total of the angles, children work out missing angles in different types of triangles.

Starting with equilateral triangles, as all the angles are equal, children learn that each angle must be $180^\circ \div 3 = 60^\circ$. They then move on to investigating isosceles triangles. Children learn that not only do isosceles triangles have two equal sides, but they also have two equal angles. They need to identify which two angles are equal in order to find the sizes of unknown angles in the triangles.

Children may need reminding of hatch mark notation to show that sides of shapes are equal in length.

Things to look out for

- Children may use a protractor to measure unknown angles, rather than working them out from given facts.
- Children may wrongly identify which two angles are equal to each other in an isosceles triangle.

Key questions

- What do the interior angles in a triangle add up to?
- If a triangle is equilateral, what do you know about its sides/angles? How can you work out the size of one of the angles?
- What are the properties of an isosceles triangle?
- Which of the angles in the triangle are equal? How do you know?
- If you know one angle in an isosceles triangle, how can you calculate the sizes of the other two angles?

Possible sentence stems

- In an equilateral triangle, all three angles are _____°.
- In an isosceles triangle, two _____ are equal and two _____ are equal.
- In a right-angled triangle, one of the angles is _____°.

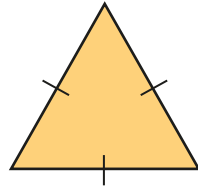
National Curriculum links

- Compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons

Angles in a triangle – special cases

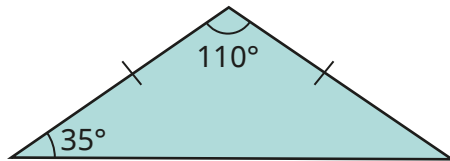
Key learning

- In an equilateral triangle, all three angles are equal.



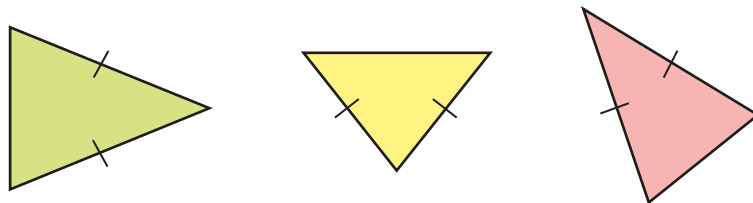
What is the size of each angle in an equilateral triangle?
How do you know?

- Work out the missing angle in the isosceles triangle.

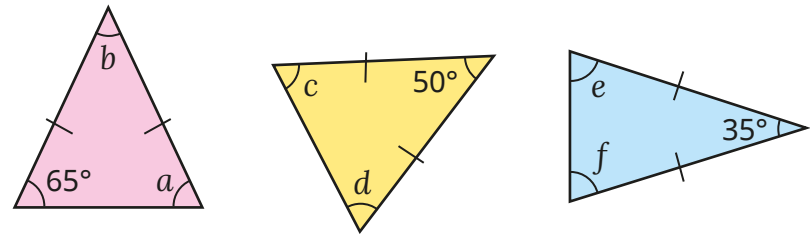


What do you notice?

- Identify which angles will be equal in each isosceles triangle.

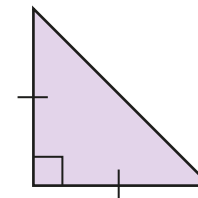


- Here are three isosceles triangles.



Work out the angles marked with letters.

- One of the angles in an isosceles triangle is 24° .
What could the other two angles be?
Find more than one possible answer.
- A right-angled triangle is also isosceles.



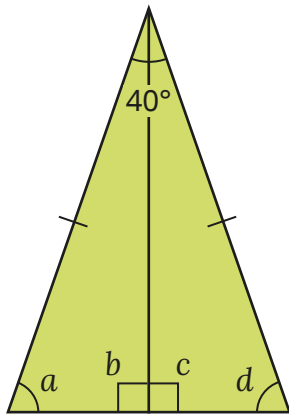
Work out the sizes of all three angles in the triangle.

Angles in a triangle – special cases

Reasoning and problem solving

How many sentences can you write to express the relationships between the angles in the triangles?

One has been done for you.



$$40^\circ + a + d = 180^\circ$$

multiple possible answers, e.g.

$$20^\circ + a + b = 180^\circ$$

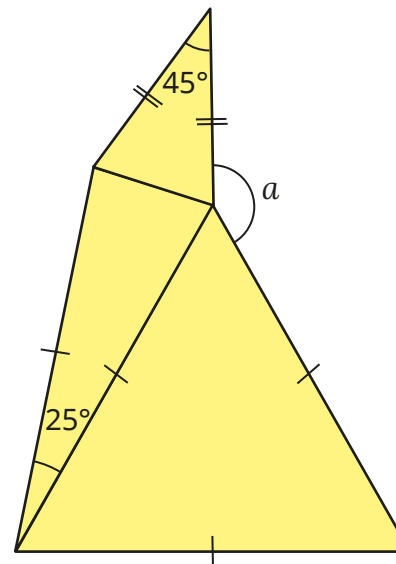
$$20^\circ + c + d = 180^\circ$$

$$b = 90^\circ, c = 90^\circ$$

$$b = c$$

$$a = d$$

The shape is made from two isosceles triangles and an equilateral triangle.



Work out the size of angle a .

$$a = 155^\circ$$

Angles in a triangle – missing angles

Notes and guidance

In this small step, children combine what they have learnt so far in this block to solve a variety of missing angle questions. By thinking about angles in different types of triangles, as well as in right angles, on a straight line and around a point, children should be able to work out the sizes of missing angles in increasingly complex problems.

Begin by recapping the rules of angles they have learnt so far, and then share a problem with the class and discuss what methods are available based on the facts they know. Work through missing angle problems that begin with one focus, but move on to examples that require knowledge of more than one rule. At each stage, ask children to explain what rules they have used to solve the problem. They will find that there are multiple ways of solving most problems, and this will consolidate their understanding of the rules.

Things to look out for

- Children may measure missing angles with a protractor, rather than working them out based on given facts.
- Children may need support to work out intermediate angles when the required angle cannot be found in one step.

Key questions

- Why can you not always find the size of the missing angle by measuring?
- What type of triangle is this? How will knowing that help you to find the value of the missing angle?
- Do you need to work out a different angle before you can work out the missing angle?
- Which angles can you work out straight away? How will that help you to work out other angles?
- What do angles in a right angle/on a straight line/around a point add up to?

Possible sentence stems

- The sum of angles in a triangle is _____°.
- The sum of angles on a straight line is _____°.
- The sum of angles around a point is _____°.
- Vertically opposite angles are _____

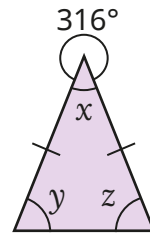
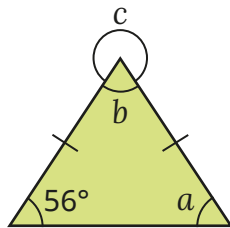
National Curriculum links

- Compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons

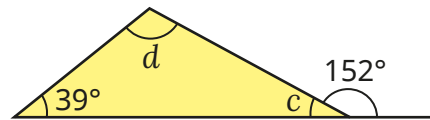
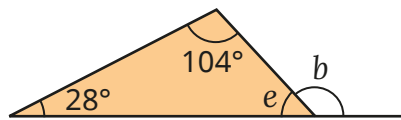
Angles in a triangle – missing angles

Key learning

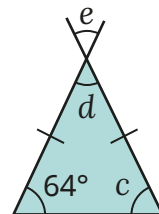
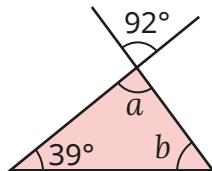
- Work out the sizes of the angles marked with letters. Explain each step in your workings.



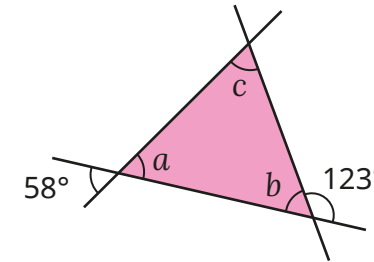
- Work out the sizes of the angles marked with letters. Explain each step in your workings.



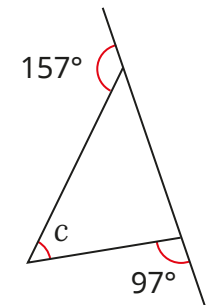
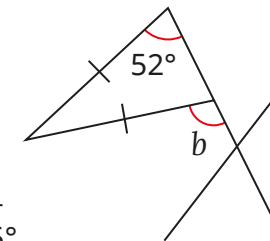
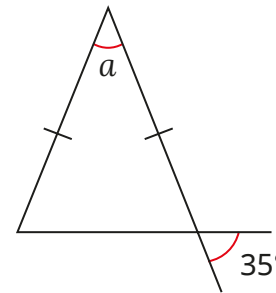
- Work out the sizes of the angles marked with letters. Explain each step in your workings.



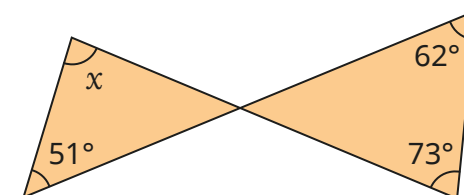
- Work out the sizes of the angles marked with letters.



- Discuss with a partner how you could work out each of the angles marked with letters. How many ways can you find to work out each one?

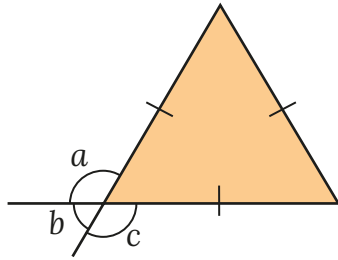


- Work out the size of angle x .

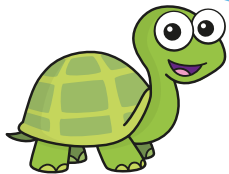


Angles in a triangle – missing angles

Reasoning and problem solving



I cannot work out the missing angles, because there are no known angles to work from.



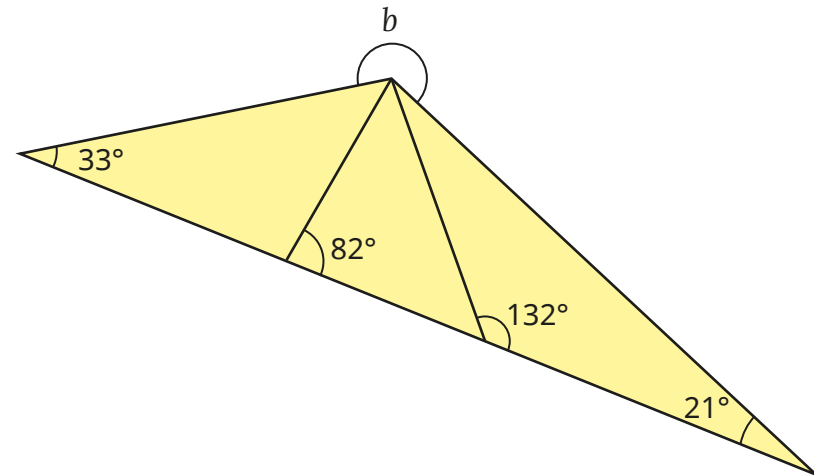
Do you agree with Tiny?

Explain your answer.

The triangle is an equilateral triangle, so each angle is 60° .

Tiny can then use other rules to work out angles a , b and c .

Work out the size of the reflex angle b .



What other angles can you work out?

$$b = 234^\circ$$

Angles in a quadrilateral

Notes and guidance

In Year 4, children explored the properties of different quadrilaterals and they should be familiar with the words “trapezium”, “rhombus”, “square”, “rectangle”, “parallelogram” and “kite”. They learnt about the equal and parallel sides in quadrilaterals, as well as which ones have right angles. In this small step, that learning is extended to include the properties of the angles in these quadrilaterals.

For a square and a rectangle, the fact that the angles add up to 360° can be worked out quickly. For other quadrilaterals, children can investigate by measuring the angles with a protractor. Show that, as any quadrilateral can be split into two triangles, the sum of the interior angles is twice that of a triangle and compare this with the totals found by measuring.

Children then move on to explore the relationships between angles in a rhombus and a parallelogram, where opposite angles are equal.

Things to look out for

- Children may incorrectly identify equal sides and/or angles.
- Children may try to use 180° instead of 360° as the sum of the angles in a quadrilateral.

Key questions

- What is a quadrilateral?
- In what ways can quadrilaterals be different from one another?
- What is the sum of the interior angles in a quadrilateral?
- What is the same/different about a rhombus and a square?
- If you know one angle in a parallelogram, how can you work out the sizes of the missing angles?

Possible sentence stems

- The sum of interior angles in any quadrilateral is _____ $^\circ$.
- A parallelogram has two pairs of equal _____ and two pairs of equal _____
- A rhombus has two pairs of equal _____ and two pairs of equal _____

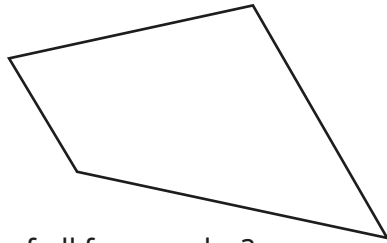
National Curriculum links

- Compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons

Angles in a quadrilateral

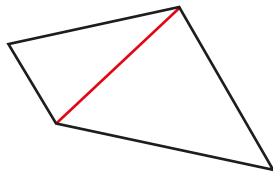
Key learning

- Measure the angles of the quadrilateral.



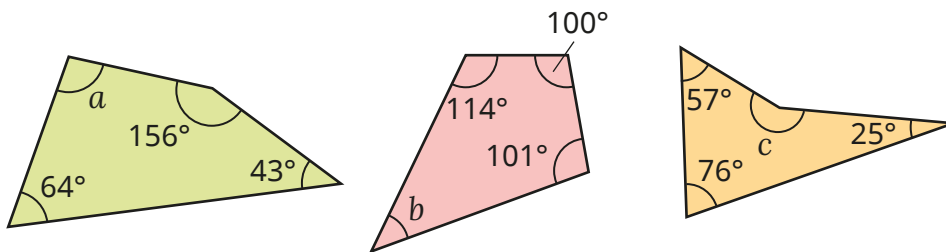
What is the sum of all four angles?

Huan draws a line on the quadrilateral to prove that the angles in any quadrilateral add up to 360° .

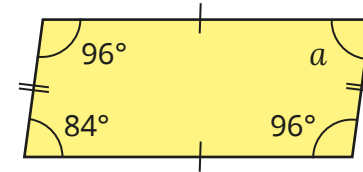


Explain Huan's reasoning.

- Work out the missing angles in the quadrilaterals.

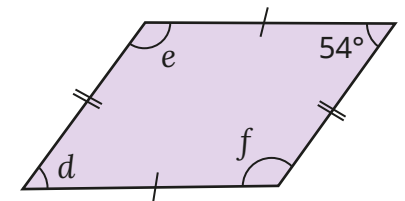
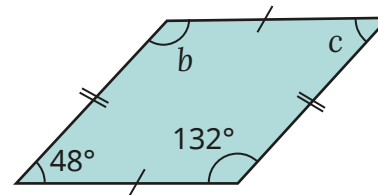


- Work out the size of angle a in the parallelogram.

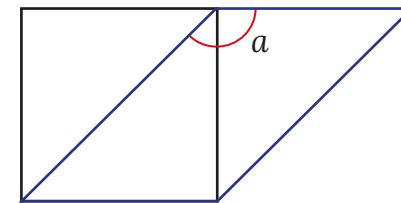


What do you notice about the opposite angles in a parallelogram?

Use this to work out the angles marked with letters in the parallelograms.



- A parallelogram has been drawn over the top of a square.

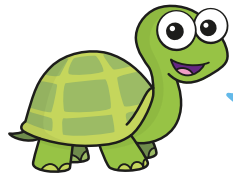


Work out the size of angle a .

Angles in a quadrilateral

Reasoning and problem solving

Tiny draws a quadrilateral with four equal sides.



My shape must be a square, so the angles are all 90° .

No

Do you agree with Tiny?

Explain your answer.

Esther draws a quadrilateral with exactly two right angles.

What types of quadrilaterals could she have drawn?

Is it possible to draw a quadrilateral with exactly three right angles?

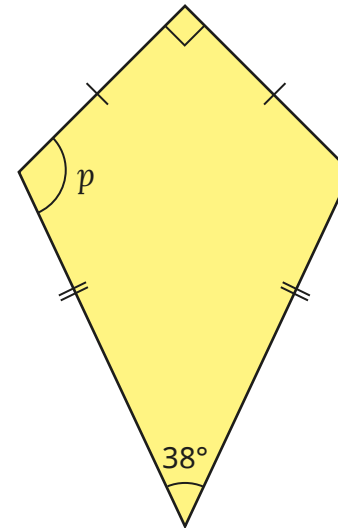
Explain your answer.

trapezium or kite

No

3 right angles sum to 270° , so the 4th angle must be $360^\circ - 270^\circ = 90^\circ$.

Here is a kite.



$p = 116^\circ$

Work out the size of angle p .

Talk to a partner about how you worked it out.

Angles in polygons

Notes and guidance

In this small step, children develop their understanding of interior angles in 2-D shapes by looking at polygons with five or more sides.

Building on the fact that a quadrilateral can be split into two triangles, so the interior angles add up to $180 \times 2 = 360^\circ$, children explore how many triangles polygons with a greater number of sides can be split into using a vertex of the polygon. They learn that the number of triangles is two fewer than the number of sides. Multiplying the number of triangles by 180° gives the sum of the interior angles in the polygon. Using this information, they can find unknown angles for any polygon. The main focus of this step is on regular polygons, where children can divide the total by the number of sides to work out the size of each angle.

Things to look out for

- Children may use a protractor instead of calculating a missing angle.
- Children may multiply the number of sides by 180° to find the sum of the interior angles.
- When looking for the number of triangles, children may draw too many triangles by drawing lines from more than one vertex of the polygon.

Key questions

- What is a polygon?
- What is the difference between a regular and an irregular polygon?
- How many triangles can you make in this polygon?
- Why is it important to draw the triangles from a single vertex?
- If the sum of interior angles in each triangle adds up to 180° , how can you work out the sum of the interior angles in the polygon?
- If you know the sum of the interior angles in a polygon, how can you use this information to find a missing angle?

Possible sentence stems

- If there are _____ sides, then there are _____ triangles.
- The sum of the angles is _____ $\times 180^\circ =$ _____ $^\circ$.
- The sum of the interior angles in a _____ is _____ $^\circ$.

National Curriculum links

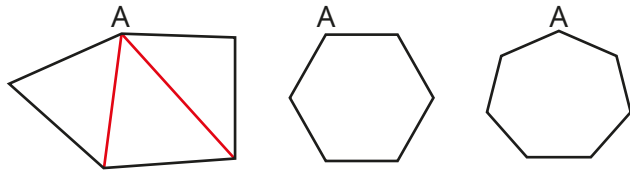
- Compare and classify geometric shapes based on their properties and sizes and find unknown angles in any triangles, quadrilaterals, and regular polygons

Angles in polygons

Key learning

- Aisha splits a pentagon into three triangles by drawing lines from vertex A.

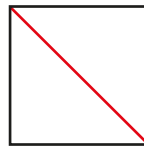
Use Aisha's method to split the other shapes into triangles.



What do you notice about the number of sides a shape has and the smallest number of triangles each one can be split into?

- Scott can make two triangles from a quadrilateral.

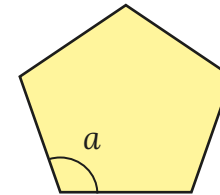
He then knows that the sum of the interior angles in a quadrilateral must be 360° .



Use Scott's method to complete the table.

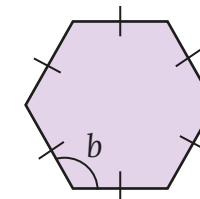
Shape	Number of sides	Number of triangles	$180 \times$ number of triangles	Sum of interior angles
square	4	2	180×2	360°
pentagon	5	3		
hexagon				
heptagon				
octagon				

- Here is a regular pentagon.

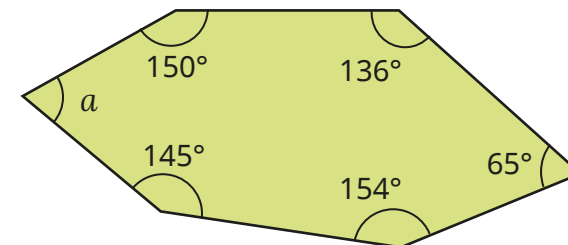


- ▶ What is the sum of the interior angles of a pentagon?
How do you know?
- ▶ What is the size of angle a ?
How do you know?

- Calculate the size of the angle b .



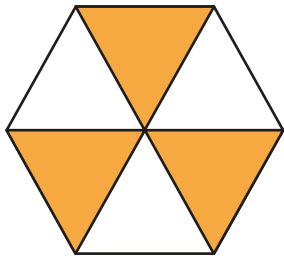
- Work out the size of angle a .



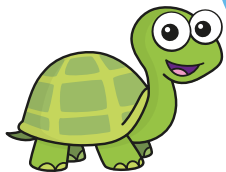
Angles in polygons

Reasoning and problem solving

Tiny draws six triangles inside a hexagon.



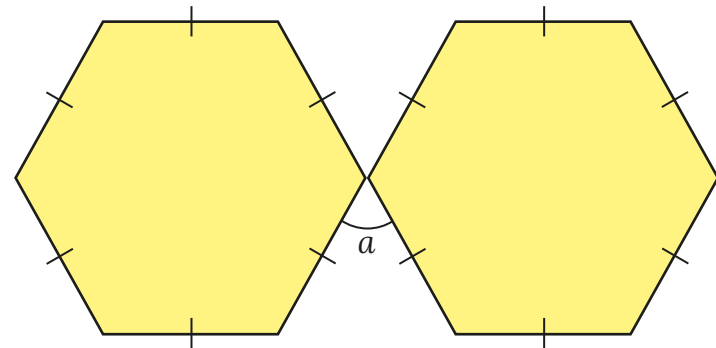
This means that the sum of angles in a hexagon is $1,080^\circ$ because $6 \times 180 = 1,080^\circ$.



Do you agree with Tiny?
Explain your answer.

No
Tiny's total includes the angles at the centre of the hexagon, not just those at the vertices.

Here are two regular hexagons.



Work out the size of angle a .

$$a = 60^\circ$$

Circles

Notes and guidance

Children used circles in pie charts in the Statistics block in the Spring term. In this small step, they develop their learning to ensure understanding of the words “radius”, “diameter” and “circumference”.

Children need to understand the importance of the centre of a circle: it is the point that is an equal distance from every part of the edge of the circle. They then move on to looking at the connection between the radius and the diameter. It is important that they realise that both of these are related to the centre. Showing examples and non-examples of radii and diameters will help to reinforce this understanding.

At this stage, children do not need to be able to calculate the circumference. It may be useful to discuss that using a piece of string around the outside of a circle, then measuring it, will give an approximate measure for this.

Things to look out for

- Children may confuse the terms “radius” and “diameter”.
- Children may think that a diameter is any line across a circle, even if it does not go through the centre.

Key questions

- What does the term “radius”/“diameter”/“circumference” mean?
- What is the relationship between the radius and the diameter of a circle?
- What point must the diameter of a circle go through?
- If you know the diameter of a circle, how can you calculate its radius?
- If you know the radius of a circle, how can you calculate its diameter?
- How can you tell if a line across a circle is a diameter or not?

Possible sentence stems

- The radius of a circle is _____ the size of the diameter of the circle.
- The diameter of a circle is _____ the size of the radius of the circle.
- All the points on the circumference of a circle are an _____ distance from the _____

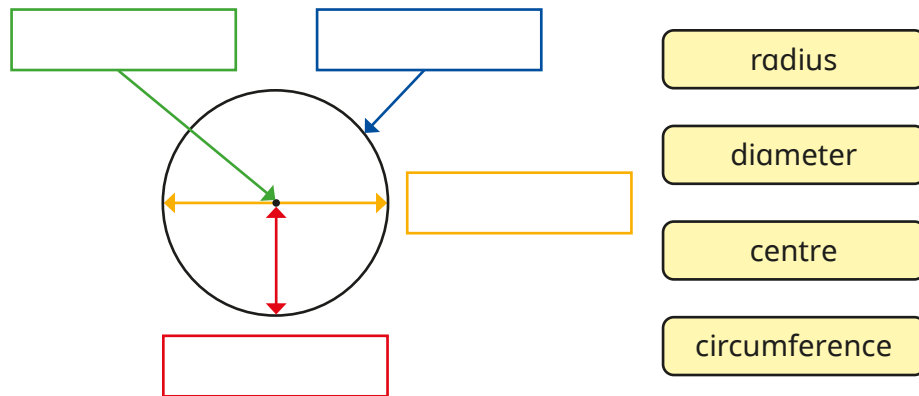
National Curriculum links

- Illustrate and name parts of circles, including radius, diameter and circumference and know that the diameter is twice the radius

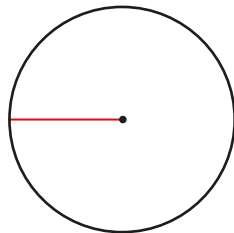
Circles

Key learning

- Use the labels to complete the diagram.



- Filip has drawn a 5 cm straight line from the centre of the circle to its edge.

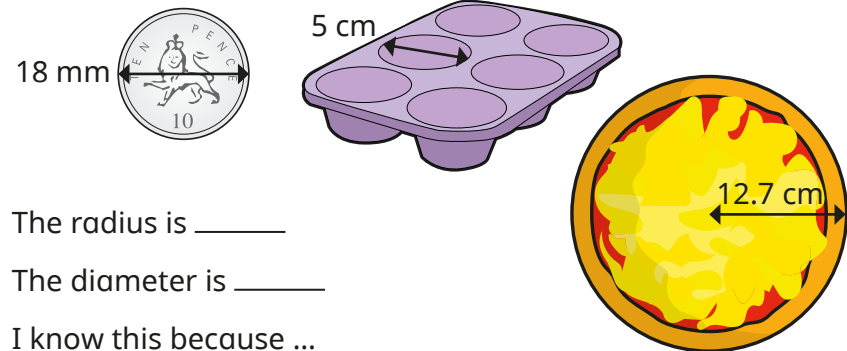


- ▶ What is the name of the line Filip has drawn?
- ▶ Explain to a partner how Filip can use this line to help him find the diameter of the circle.

- Complete the table.

Radius	Diameter
26 cm	
	37 mm
2.55 m	
	99 cm
	19.36 cm

- Find the radius and the diameter for each object.



The radius is _____

The diameter is _____

I know this because ...

- If the radius of a circle is r and the diameter is d , which formula shows the relationship between the radius and diameter of the circle?

$$2r = d$$

$$2d = r$$

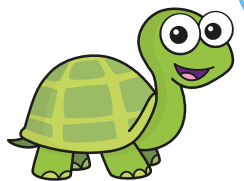
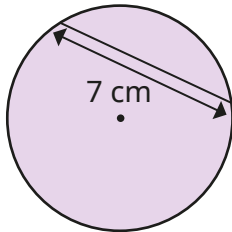
$$r + 2 = d$$

$$d + 2 = r$$

Circles

Reasoning and problem solving

Tiny is trying to find the radius of the circle.



I know that the diameter is 7 cm, so the radius is 3.5 cm.

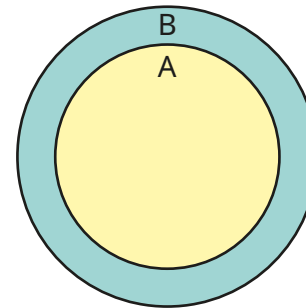
Do you agree with Tiny?
Explain your answer.

No
The diameter needs to pass through the centre of the circle and this line does not.

Circle A has been drawn on top of circle B.



The diameter of circle A is $\frac{3}{4}$ the diameter of circle B.



If the diameter of circle B is 12 cm, what is the diameter of circle A?

If the diameter of circle A is 12 cm, what is the diameter of circle B?

If the radius of circle B is 6 cm, what is the radius of circle A?

If the radius of circle A is 6 cm, what is the diameter of circle B?

- 9 cm

- 16 cm

- 4.5 cm

- 16 cm

Draw shapes accurately

Notes and guidance

In this small step, children use skills learnt so far in this block to accurately draw shapes when given specific dimensions.

Children begin drawing simple shapes that can be done on squared paper, such as rectangles and right-angled triangles where the base and height are given. This could be extended to drawing shapes where the perimeter and some of the sides are known.

Children then produce an accurate drawing of a shape with known angles. They may need to begin by practising using a protractor. Children should work systematically, starting with a side and then drawing the angle(s) from the correct end(s). They should also use their understanding of the features of different quadrilaterals and triangles to recreate these accurately.

This step is a good opportunity to revisit converting between centimetres and millimetres.

Things to look out for

- Children may need support to decide which part of the shape to draw first.
- Children may start from the wrong end of the scale on a protractor.

Key questions

- How can you use squared paper to draw a shape with right angles?
- What tools can you use to help you draw a shape accurately?
- What do you know about the shape that will help you to draw it accurately?
- Which part of the shape can you draw first? Then what can you draw?
- How can you check if your shape is drawn accurately?
- What labels can you add to your drawing?
- Which scale on the protractor do you need to use?

Possible sentence stems

- If the perimeter of the rectangle is _____ cm and one side is _____ cm, then the other sides must be _____ cm, _____ cm and _____ cm.
- If an angle is _____ than 90° , I need to use the _____ scale on the protractor.

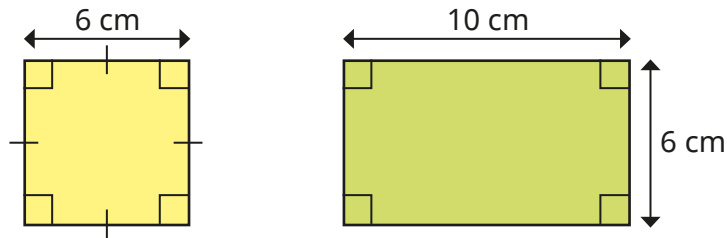
National Curriculum links

- Draw 2-D shapes using given dimensions and angles

Draw shapes accurately

Key learning

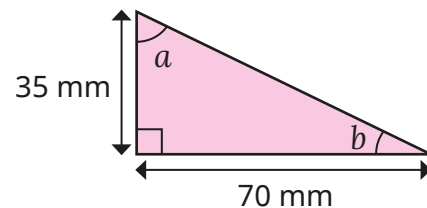
- Draw the shapes accurately on squared paper.



- Draw the right-angled triangle accurately on squared paper.

What is the missing length?

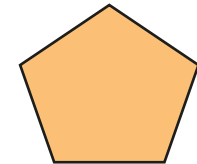
Measure the sizes of angles a and b .



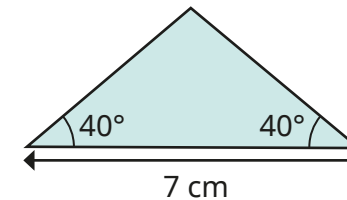
- Draw the shapes accurately on squared paper.
 - ▶ a square with a perimeter of 16 cm
 - ▶ a rectangle with an area of 20 cm^2
 - ▶ a right-angled triangle with a height of 8 cm and a base of 6 cm
- The sides of a right-angled triangle are 3 cm, 4 cm and 5 cm. Draw the triangle and measure the sizes of its angles. Label the triangle with as much information as you can.

- What is the size of each interior angle of the regular polygon?

Accurately draw a regular pentagon with a side length of 5 cm.



- Write a step-by-step plan to draw the triangle.



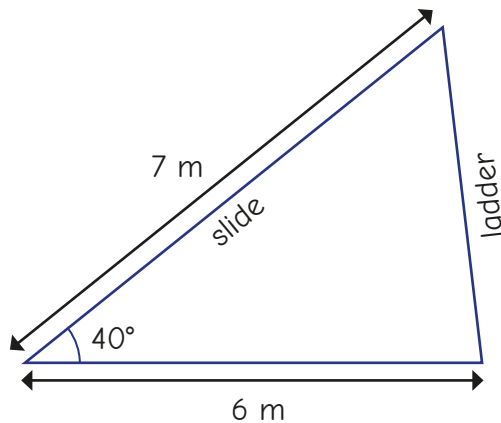
Use your plan to make an accurate copy of the triangle.

- Use a ruler and a protractor to draw the shapes. Label the information that is given to you on the shape, as well as any equal or parallel lines.
 - ▶ a right-angled triangle with one angle of 38°
 - ▶ a parallelogram with two angles of 40° and two sides of 6 cm
 - ▶ an equilateral triangle with a perimeter of 21 cm
 - ▶ an irregular pentagon with a perimeter of 75 cm and two interior right angles

Draw shapes accurately

Reasoning and problem solving

Mr Hall is designing a slide for the playground.



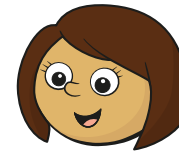
approximately
4.5 m

Use a scale of 1 cm to represent 1 m.

Draw a scale diagram.

Use the diagram to find out approximately how long the ladder needs to be.

Kim has drawn a scalene triangle.



- Angle a is the greatest angle.
- Angle b is 20° larger than angle c .
- Angle c is 70° smaller than angle a .

Use a bar model to help you calculate the size of each angle.

Then draw Kim's triangle.

Is there more than one way to draw the triangle?

$$a = 100^\circ$$

$$b = 50^\circ$$

$$c = 30^\circ$$

These angles work with different side lengths.

Nets of 3-D shapes

Notes and guidance

In the final small step of this block, children learn that they can make a 3-D shape using knowledge of the 2-D shapes that make up its faces.

Children should be familiar with 3-D shapes from earlier years, but you may need to remind them how to describe these shapes using edges, faces, vertices and curved surfaces. They should explore this step practically, starting with nets of a cube, made up of six squares, and investigating which arrangements will and will not fold to make a cube. Children can then move on to looking at other 3-D shapes and what 2-D shapes are needed to make their nets. Again, they first need to explore this with cut-out nets, which will help them to become more adept at visualising how nets fold up. Children can then work from a 3-D shape to decide how the net will look.

Things to look out for

- Children may have the correct number of 2-D shapes in a net, but not in an arrangement that will create the correct shape.
- Children may need a reminder of vocabulary such as “prism” when naming 3-D shapes.

Key questions

- How many faces does a _____ have? What shapes are they?
- What is the difference between a 2-D and a 3-D shape?
- What 2-D shapes are needed to create the net of a _____?
- What 3-D shape will this net create?
- Which two faces of the 3-D shape made from this net will be opposite each other?
- How many different ways can you arrange the faces of the net so that it still folds up to make the _____?

Possible sentence stems

- The net needed to make a _____ will contain _____ _____ and _____ _____ (e.g. triangular prism, three rectangles, two triangles)
- I know that this net will make a _____ because ...

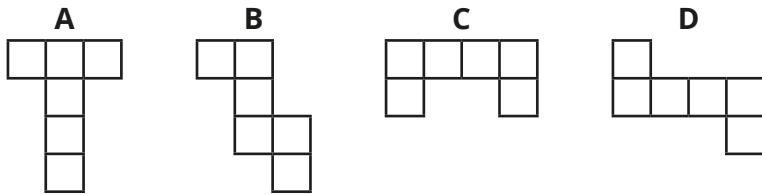
National Curriculum links

- Recognise, describe and build simple 3-D shapes, including making nets

Nets of 3-D shapes

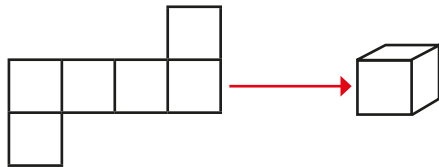
Key learning

- Which nets will fold up to make a cube?

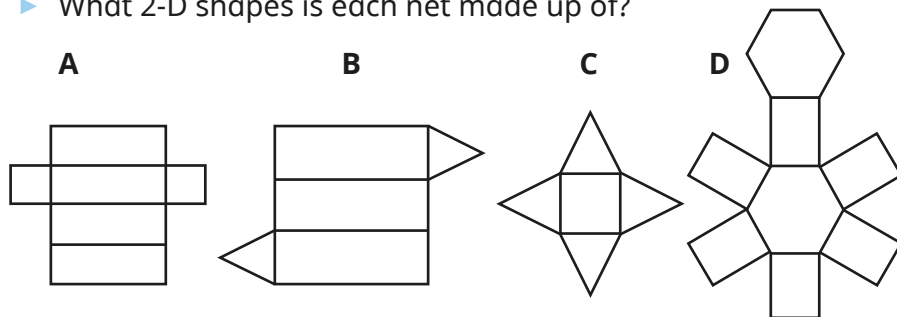


Investigate other possible nets for a cube.

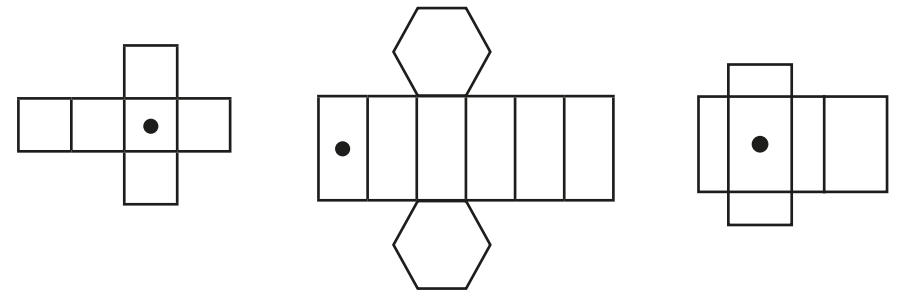
- The net of a cube is made up of six squares.



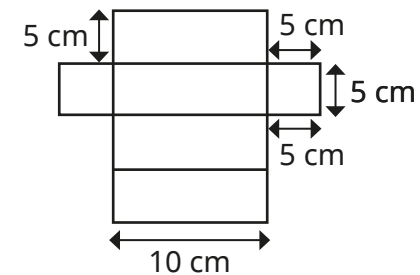
- ▶ Which 3-D shapes will these nets make?
- ▶ What 2-D shapes is each net made up of?



- Draw another dot on each net so that the dots are on opposite faces when the net is folded to make the 3-D shape.



- Draw the net accurately on squared paper.



- Draw nets for the 3-D shapes described.
 - The faces are made up of a square and four triangles.
 - The faces are made up of rectangles and triangles.

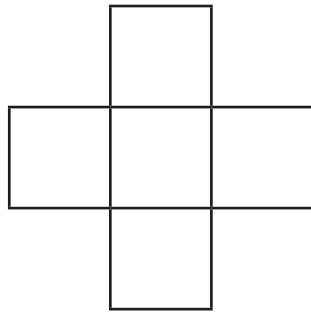
Find as many shapes as you can for each description.

Make the 3-D shapes from your nets.

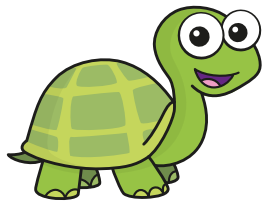
Nets of 3-D shapes

Reasoning and problem solving

Tiny is making nets.



This net will make a cube.

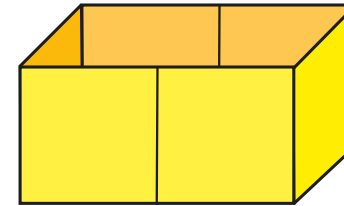


Do you agree with Tiny?

Explain your answer.

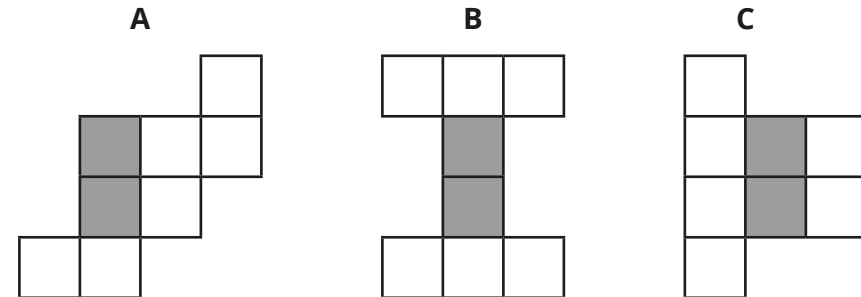
No
A cube has six faces, but the net only has five.

Here is an open box.



Which nets will fold to make the box?

The grey squares show the base.



B and C

Summer Block 2

Position and direction

Small steps

Step 1

The first quadrant

Step 2

Read and plot points in four quadrants

Step 3

Solve problems with coordinates

Step 4

Translations

Step 5

Reflections

The first quadrant

Notes and guidance

Children were first introduced to a coordinate grid in Year 4. That learning is revisited in this small step, with children looking at the first quadrant, where both the x - and y -coordinates are positive.

Begin by recapping what the coordinate grid is and the names of the two axes, x and y . Then consider points on the grid. Discuss how children can find the coordinates for a given point, reading the first value on the x -axis and the second value on the y -axis. Children then move on to plotting points with given coordinates. Ensure that children understand the importance of the order of the values.

Children draw shapes on a coordinate grid, suggesting possible coordinates for vertices of different shapes. Finally, they solve problems in the first quadrant without the support of grid lines, using given coordinate information to find the coordinates of other points.

Things to look out for

- Children may confuse the x - and y -values of the coordinates and read or plot them in the wrong order.
- Children may think a coordinate refers to a square on the grid rather than a single point.

Key questions

- What is a coordinate grid?
- What is the name of the horizontal/vertical axis?
- What are the coordinates of this point?
- Which axis do you look at first when finding the coordinates of a point?
- Where does the point _____ go on the grid?
- What do you notice about all the points that are on a horizontal/vertical line?
- How can you work out the missing coordinate(s)?

Possible sentence stems

- The first value in a pair of coordinates is for the _____-axis and the second value is for the _____-axis.
- The x -coordinate of the point is _____ and the y -coordinate is _____
The point is (_____, _____).

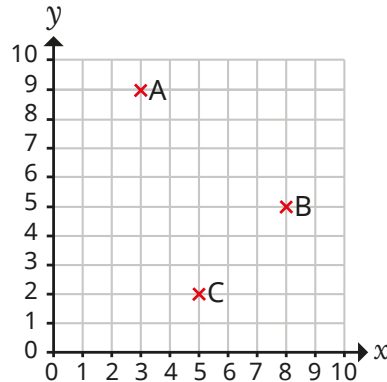
National Curriculum links

- Describe positions on the full coordinate grid (all four quadrants)

The first quadrant

Key learning

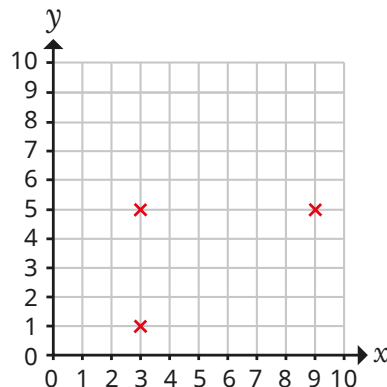
- Here is a coordinate grid.



- ▶ What are the coordinates of the points A, B and C?
- ▶ Plot points D, E and F on the grid.

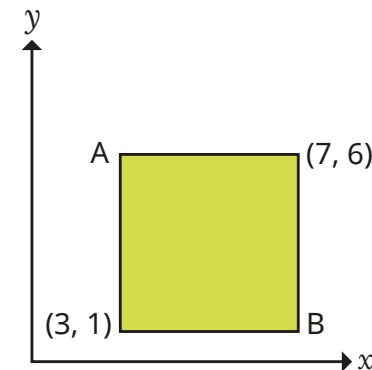
D (1, 5) E (5, 5) F (0, 8)

- Tommy is drawing a rectangle on a coordinate grid.



Find the coordinates of the fourth vertex of the rectangle.

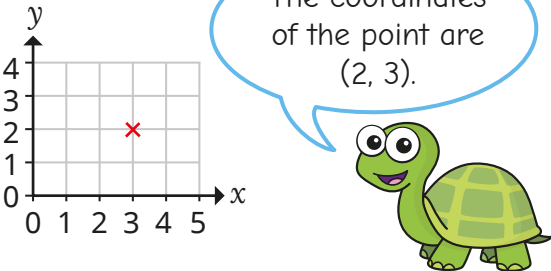
- Plot the points (7, 1), (7, 4) and (10, 1) on a coordinate grid. Join the points to form a polygon. What polygon have you drawn?
- Plot four points on a coordinate grid to make a square. What are the coordinates of the vertices? What patterns can you see? How do you know that the shape is a square?
- The diagram shows the coordinates of two vertices of a rectangle.



What are the coordinates of the other two vertices?
How did you work out the coordinates?

The first quadrant

Reasoning and problem solving



The coordinates of the point are (2, 3).

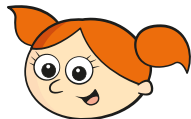
Do you agree with Tiny?
Explain your answer.

No

(2, 2)

(3, 3)

(7, 7)



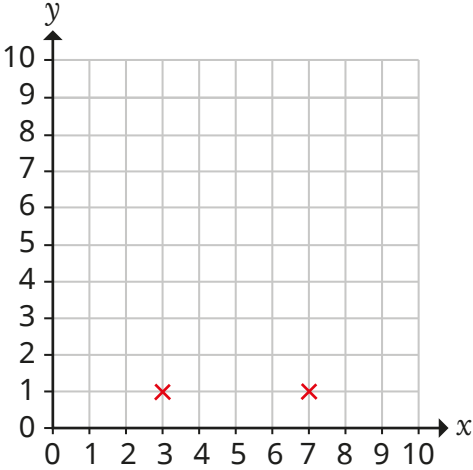
Alex thinks that when she joins these points, they will make a straight line.

Do you agree with Alex?
Explain your answer.

Yes

Huan wants to draw an isosceles triangle on the coordinate grid.

He has already plotted the points for two of the vertices.



What could the coordinates of the third vertex be?
How many different answers can you find?

(5, a), where a is not equal to 1
(3, 5)
(7, 5)

Read and plot points in four quadrants

Notes and guidance

In this small step, children extend their understanding of the coordinate grid to include all four quadrants. It may be helpful to refer to these as the first (top-right), second (top-left), third (bottom-left) and fourth (bottom-right) quadrants.

Show children that the x - and y -axes can both be extended through zero into negative numbers. Children plot points in each of the “new” quadrants in turn. Model that the process is the same as for the first quadrant, and emphasise that the axes behave in the same way as number lines with positive and negative numbers, which children are already familiar with. Children should recognise the pattern of positive and negative coordinates that belong in each quadrant.

When children are comfortable with points in each of the quadrants, they move on to drawing shapes in the coordinate grid, using all of the quadrants. Finally, they determine which quadrant a point with given coordinates is in, without the use of a grid to support them.

Things to look out for

- Children may confuse the x - and y -values of the coordinates and read or plot them in the wrong order.
- Children may ignore or omit the negative sign.

Key questions

- Which axis do you look at first when finding the coordinates of a point?
- What are the coordinates of the point?
- What are the coordinates of the vertices of the shape?
- Where does the point _____ go on the grid?
- How do you know if the x -value/ y -value is positive or negative?
- What do you notice about the coordinates in the first/second/third/fourth quadrant?

Possible sentence stems

- The first value in a pair of coordinates is for the _____-axis and the second value is for the _____-axis.
- The x -coordinate of the point is _____ and the y -coordinate is _____. The point is (_____, _____).
- The x -coordinate of a point in the _____ quadrant is _____
- The y -coordinate of a point in the _____ quadrant is _____

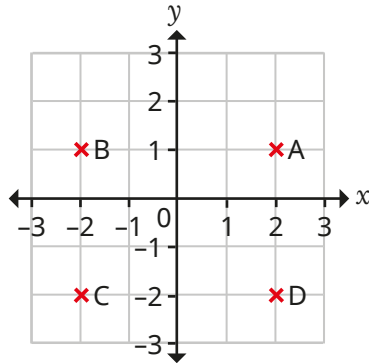
National Curriculum links

- Describe positions on the full coordinate grid (all four quadrants)

Read and plot points in four quadrants

Key learning

- What are the coordinates of the four points?



How did you work them out?

Compare answers with a partner.

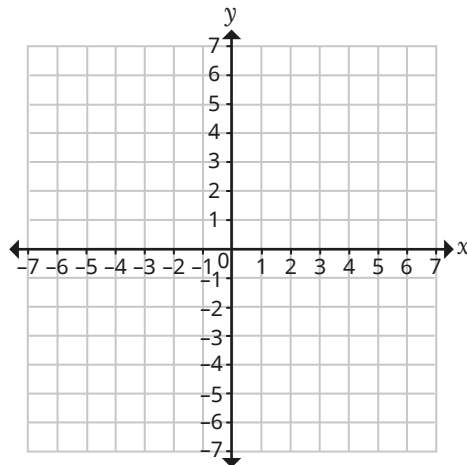
- Plot and label the points on the grid.

D (4, 5)

E (-3, 2)

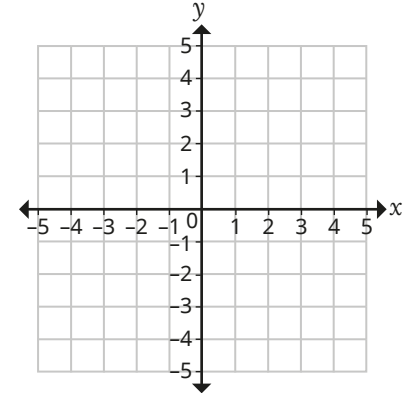
F (6, -5)

G (-1, -7)



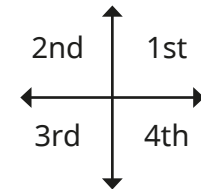
- Draw a polygon with vertices at $(-2, 2)$, $(-4, 2)$, $(-4, -2)$ and $(-2, -3)$.

What is the mathematical name of the shape?



- Draw a coordinate grid with each axis from -5 to 5
Draw a square with a vertex in each quadrant.
Write the coordinates of the vertices.

- Write the coordinates of four points, one in each quadrant.



- Without plotting points P, Q, R and S, describe which quadrant each point is in.

P $(-8, 3)$

Q $(8, -3)$

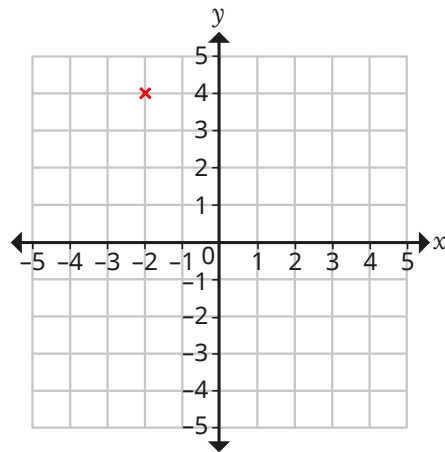
R $(8, 3)$

S $(-8, -3)$

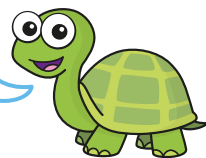
Read and plot points in four quadrants

Reasoning and problem solving

A point is plotted on a coordinate grid.



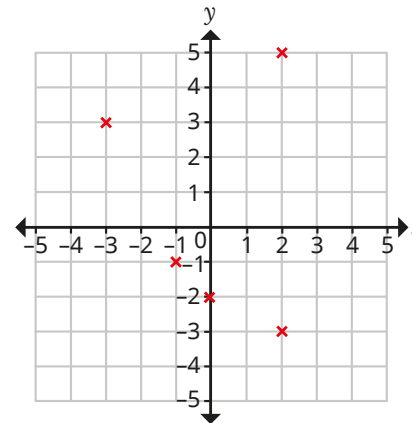
The coordinates of the point are (2, 4).



Do you agree with Tiny?
Explain your answer.

No

Amir plots five points on a grid and writes their coordinates.



(2, -5) (3, -3) (-1, -1)
(-2) (2, -3)

Mark Amir's work and make any corrections necessary.

Discuss with a partner what mistakes Amir might have made and why he might have made them.

(2, -5) ✗ (2, 5)
(3, -3) ✗ (-3, 3)
(-1, -1) ✓
(-2) ✗ (0, -2)
(2, -3) ✓

Solve problems with coordinates

Notes and guidance

In this small step, children use their knowledge of coordinates in four quadrants to solve problems, such as working out the coordinates of vertices of polygons.

Children need to be secure in reading and plotting coordinates in all four quadrants. They consider horizontal and vertical lines that go through a known coordinate, using the fact that if they know the x -coordinate of a point on a vertical line, then every point on that line will have the same x -coordinate. Similarly, every point on a horizontal line will have the same y -coordinate. Children then use this information to help find missing coordinates on shapes, both on grids with gridlines and on those without. Finally, they use the properties of shapes to solve problems on coordinate grids, for example using the fact that the opposite sides of a rectangle are equal in length.

Things to look out for

- Some children may need the support of gridlines to work out the coordinates of a point.
- If children confuse the x - and y -values of the coordinates of a point, then coordinates derived from this point will also be incorrect.

Key questions

- Which axis do you look at first when finding the coordinates of a point?
- What do you know about the coordinates of all points on the x -axis/ y -axis?
- If you know the coordinates of a point, what do you know about the coordinates of a point that lies on the vertical/horizontal line that passes through the point?
- How can you use the coordinates of these two vertices to work out the coordinates of the other vertices?

Possible sentence stems

- On a horizontal line, the _____-value of the coordinates of any point will remain the same.
- On a vertical line, the _____-value of the coordinates of any point will remain the same.
- If the x -/ y -coordinate of the vertex is _____, I know that the x -/ y -coordinate of the other vertex must be _____

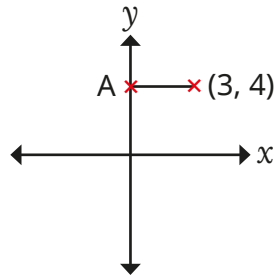
National Curriculum links

- Describe positions on the full coordinate grid (all four quadrants)

Solve problems with coordinates

Key learning

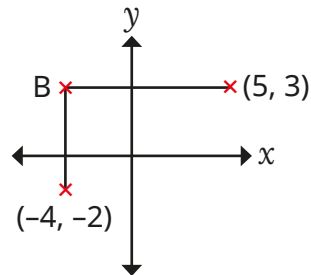
- A horizontal line is drawn between two coordinates on a grid.



What are the coordinates of point A?

How do you know?

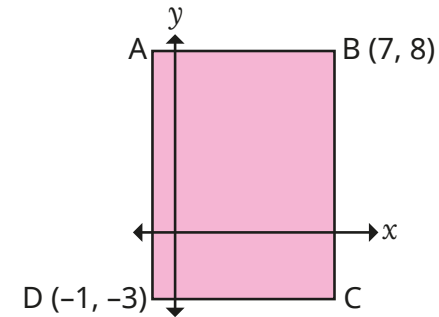
- A horizontal line goes through $(5, 3)$.
A vertical line goes through $(-4, -2)$.
The horizontal line meets the vertical line at point B.



What are the coordinates of point B?

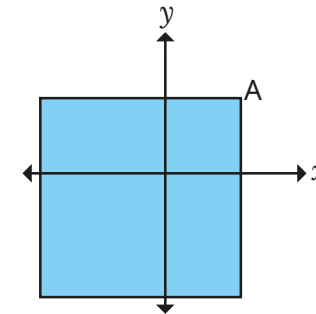
How did you find the coordinates?

- ABCD is a rectangle.



Work out the coordinates of A and C.

- A square has been drawn on a coordinate grid.
The square has a perimeter of 20 units.
Vertex A is at $(2, 2)$.



What are the coordinates of the other three vertices of the square?

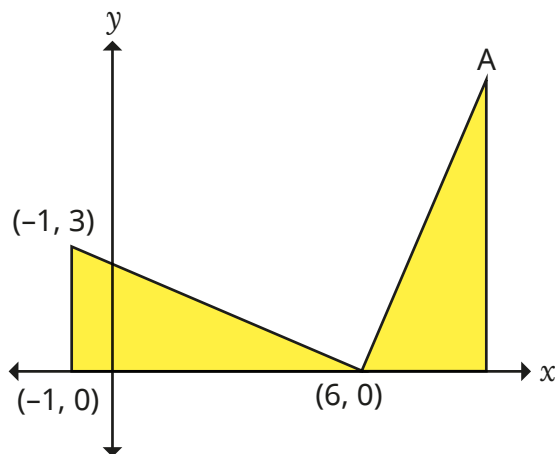
Solve problems with coordinates

Reasoning and problem solving

The diagram shows two identical triangles.

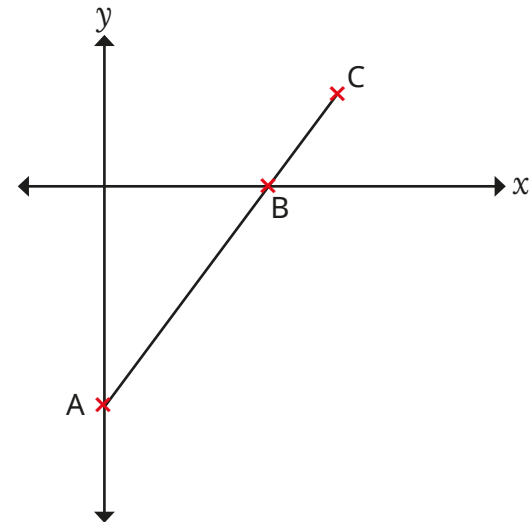
The coordinates of three points are shown.

Work out the coordinates of A.



$(9, 7)$

ABC is a straight line.



$(12, 5)$

A is the point $(0, -10)$.

B is the point $(8, 0)$.

The distance from A to B is two-thirds of the distance from A to C.

Work out the coordinates of C.

Translations

Notes and guidance

Now that children have a good understanding of coordinates in all four quadrants, in this small step they move on to translating points and shapes on a coordinate grid. They first experienced translation on a coordinate grid in Year 4, and that learning is now extended to translate in all four quadrants.

Begin by recapping that translating points means to move them. Look first at translations in one direction, either left/right or up/down, before moving on to translations in both directions. Once children have recapped translating single points on a grid, they explore translating shapes, applying the same translation to each vertex of the shape. They should see that the shape looks identical after being translated, but is in a different position on the coordinate grid. Give children opportunities to describe translations as well as perform them. Encourage children to explore the effect of translations on the coordinates.

Things to look out for

- Children may look at the gap between shapes, instead of how far a specific vertex has been translated.
- Children may not give the direction of the translation and/or confuse left and right.
- Children may confuse translation and reflection.

Key questions

- What does “translation” mean?
- How can you translate a point?
- What will the shape look like when it has been translated?
- Which point on the shape will you translate first?
- Will each vertex on a shape be translated in the same way?
- How can you describe the translation?

Possible sentence stems

- Shape A has been translated _____ squares to the right/left and _____ squares up/down.
- (_____, _____) translated _____ squares to the right/left is (_____, _____).
- (_____, _____) translated _____ squares up/down is (_____, _____).

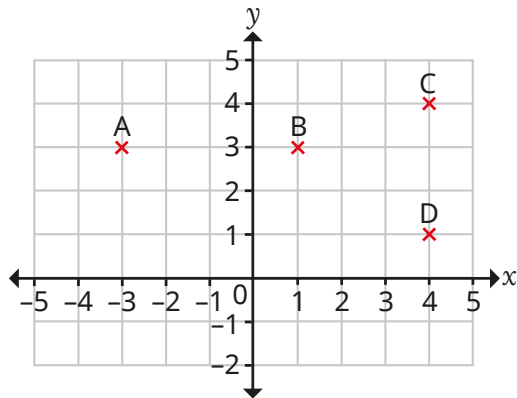
National Curriculum links


- Draw and translate simple shapes on the coordinate plane, and reflect them in the axes

Translations


Key learning

- Four points have been marked on a grid.



▶  The translation from point A to point B is 4 squares to the right.

What is the translation from point C to point D?

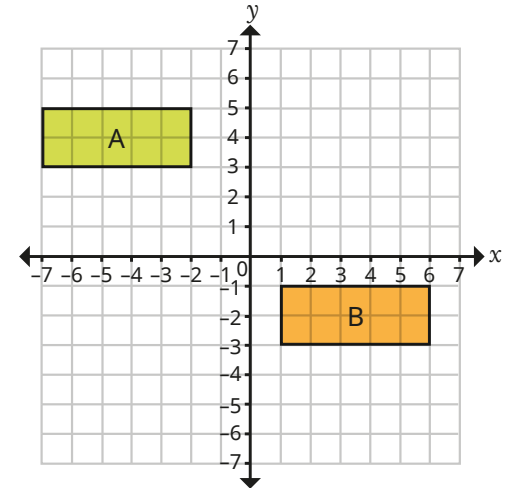
▶  The translation from point B to point D is 3 squares to the right and 2 squares down.

What is the translation from point D to point A?

- ▶ Point C is translated 3 squares to the left and 2 squares down.

What are the coordinates of the new point?

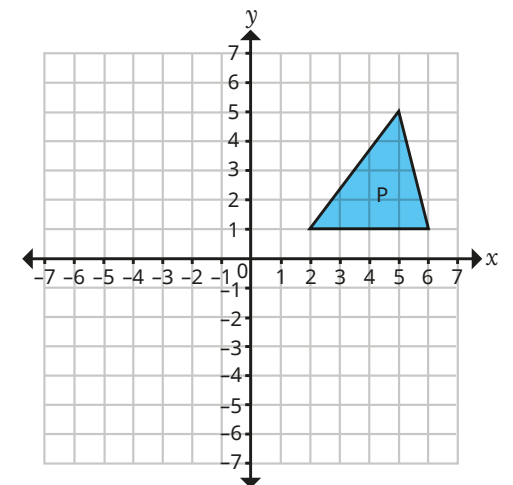
- Describe the translation from shape A to shape B.



What do you notice about shapes A and B?

- Triangle P is translated 6 squares to the left and 3 squares down.

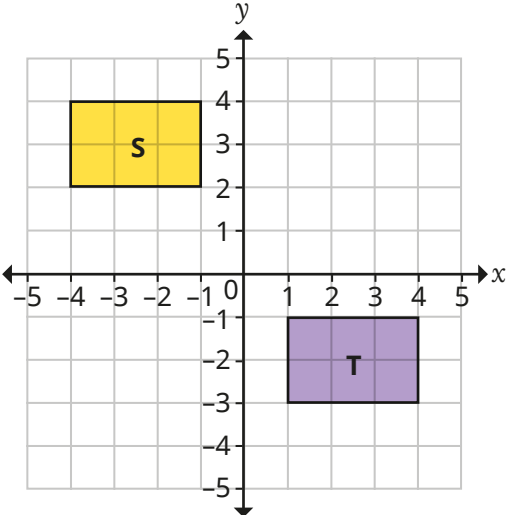
Draw the new position of the triangle and label it Q.



What do you notice about triangles P and Q?

Translations

Reasoning and problem solving



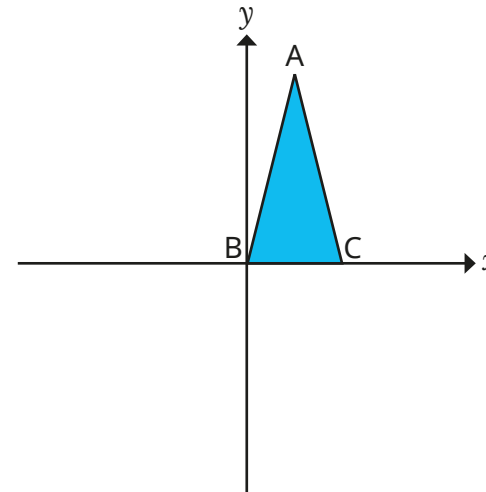
Rectangle S has been translated 2 squares to the right and 3 squares down to give rectangle T.

Do you agree with Tiny?
Explain your answer.

No

An isosceles triangle is drawn on a coordinate grid.

Vertex A has the coordinates (2, 5) and vertex B is at (0, 0).



The triangle is translated 4 to the right and 6 down.

What are the new coordinates of vertex C?

(8, -6)

Reflections

Notes and guidance

Children reflected shapes in the first quadrant of coordinate grids in Year 5, both with gridlines and without, using lines parallel to the x - or y -axis. In this small step, that learning is revisited and extended to include reflections across all four quadrants.

It can be useful to use mirrors to explore reflection and to see that a reflected image looks identical to the original image, but faces the opposite direction. Start with reflecting points and shapes on a coordinate grid in the x - or y -axis. Children should count how far away each vertex is from the axis and use this to work out the coordinates of each vertex in the reflected shape. They could then be stretched to reflect shapes in lines that are parallel to each axis. This should be done both with gridlines and without, giving children the opportunity to work out reflections both by counting squares and by calculation.

Things to look out for

- Children may confuse translation and reflection.
- Children may draw the reflection of a shape in the same orientation as the original shape.
- Children may miscount the distances to/from the mirror line.

Key questions

- How is reflecting similar to translating? How is it different?
- How does reflecting one vertex at a time make it easier to reflect the whole shape?
- How far away is the vertex from the mirror line? How far away does the corresponding vertex need to be from the mirror line?
- How can you check if the reflected shape looks like it is in the correct place?
- Does the reflection of a shape always, sometimes or never face the same way as the original shape?

Possible sentence stems

- Shape _____ has been reflected in the _____-axis.
- The vertex is _____ squares away from the mirror line, so the corresponding vertex also needs to be _____ squares away from the mirror line.

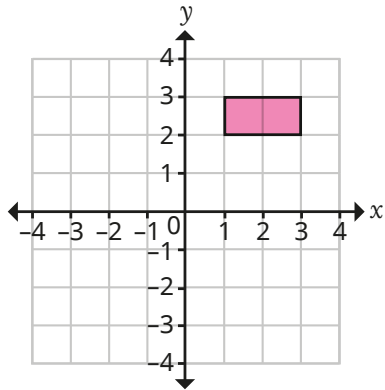
National Curriculum links

- Draw and translate simple shapes on the coordinate plane, and reflect them in the axes

Reflections

Key learning

- Mo is reflecting this rectangle in the x -axis.



I will reflect one vertex at a time. I can count how far away it is from the x -axis, then plot the point that far below the x -axis.

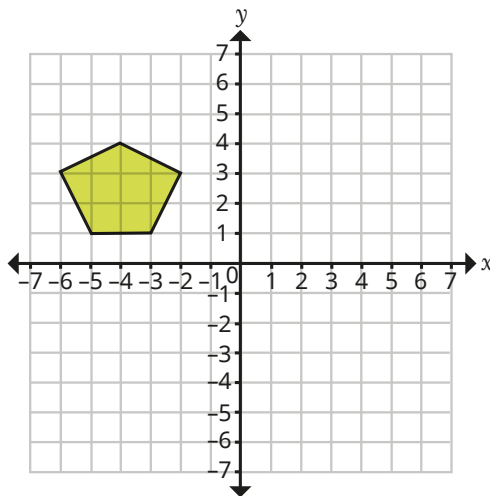
Use Mo's method to complete the reflection.

What are the coordinates of each vertex of the reflected rectangle?

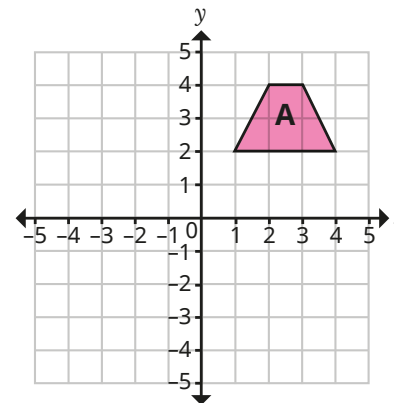
What do you notice?

- Reflect this shape in the x -axis and in the y -axis.

What do you notice about the reflections?



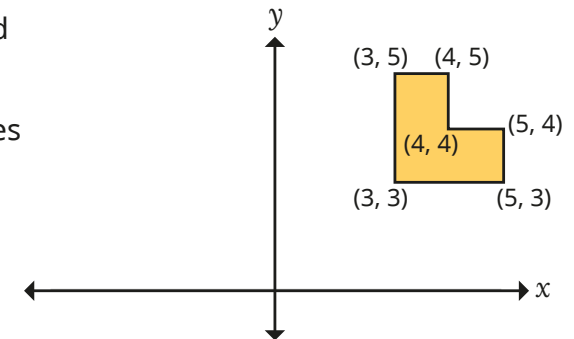
- Reflect trapezium A in the x -axis. Label the new trapezium B.
 - Reflect trapezium B in the y -axis. Label the new trapezium C.
- Complete the table with the coordinates of the vertices of each shape.



A	B	C
(1, 2)		
(4, 2)		
(3, 4)		
(2, 4)		

What do you notice?

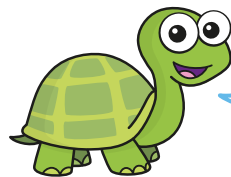
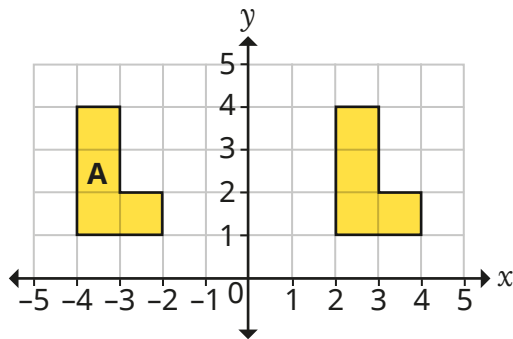
- The hexagon is reflected in the y -axis.
- Work out the coordinates of the vertices of the reflected shape.



Reflections

Reasoning and problem solving

Tiny is reflecting shapes.



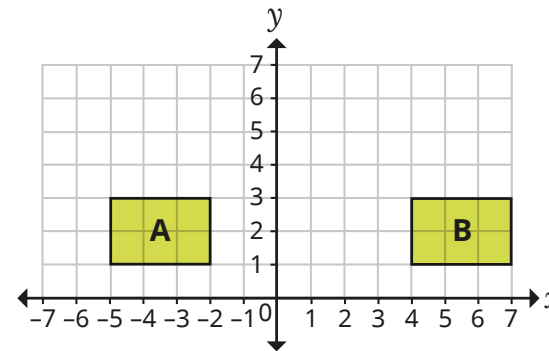
I have reflected A in the y-axis.

Do you agree with Tiny?
Explain your answer.



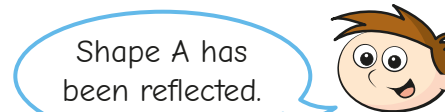
No

Shapes A and B are on a coordinate grid.



Whitney

Shape A has been translated.



Teddy

Shape A has been reflected.

Who is correct?

Explain your answer.

Both could be correct.

Shape A could have been reflected in the vertical line through (1, 0) or translated 9 squares to the right.